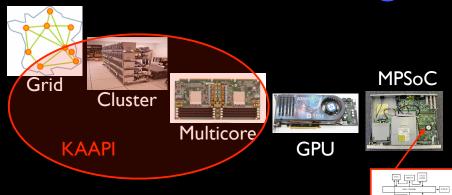
# Scheduling parallel program with Work stealing

Vincent Danjean, Vincent.Danjean@imag.fr

MOAIS project, INRIA Grenoble Rhône-Alpes Seminar at UFRGS, Porto Alegre, Brazil

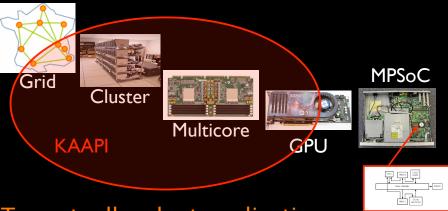


## **Moais Positioning**



To mutually adapt application and scheduling

## **Moais Positioning**



To mutually adapt application and scheduling

## **MOAIS** group

- Funded by INRIA, CNRS, UJF, INPG
- Part of LIG (Laboratoire d'Informatique de Grenoble)
  - http://moais.imag.fr
- Jean-Louis Roch: project Leader
- 10 researchers
- 18 PhD students

#### Research actions

- Scheduling [Denis Trystram]
  - multi-objectif criteria, malleable and moldable model
- Parallel Algorithms [Jean-Louis Roch]
  - adaptive algorithms
- Virtual Reality [Bruno Raffin]
  - interactive simulation
- Runtime for HPC [Thierry Gautier]
  - grid and cluster, multi-processor

#### **Outline**

- Athapascan / Kaapi a software stack
- Foundation of work stealing
- Controls of the overheads

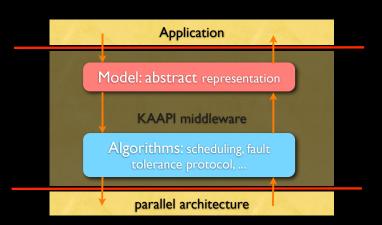
Experiments with STL algorithms

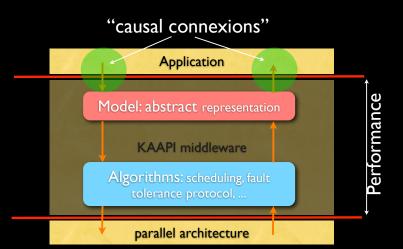
#### Goal

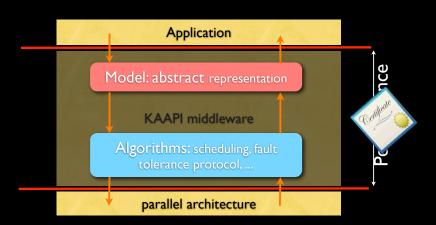
 Write once, run anywhere... with guaranteed performance

- Problem: heterogeneity
  - variations of the environment (#cores, speed, failure...)
  - irregular computation









## **API: Athapascan**

- Global address space
  - Creation of objects in a global address space with 'shared' keyword
- Task = function call
  - Creation with 'Fork' keyword (≠ unix fork) ~ Cilk spawn
  - Tasks only communicate through shared objects
  - Task declares access mode (read, write, concurrent write, exclusive) to shared objects
- Automatic scheduling
  - Work stealing or graph partitioning
- → 'Sequential' semantics
- C++ library, not a language extension
  - Clanguage extension + compiler was prototyped

## Fibonacci example

```
struct Fibonacci {
  void operator()( int n, al::Shared w<int> result )
     if (n < 2) result.write( n );
     else {
        a1::Shared<int> subresult1;
        a1::Shared<int> subresult2;
        al::Fork<Fibonacci>()(n-1, subresult1);
        al::Fork<Fibonacci>()(n-2, subresult2);
        a1::Fork<Sum>()(result, subresult1, subresult2);
struct Sum {
  void operator()( al::Shared w<int> result,
                    a1::Shared r<int> sr1,
                    a1::Shared r<int> sr2 )
  { result.write( sr1.read() + sr2.read() ); }
```

◆ロト 4周ト 4 ヨト 4 ヨ り 9 ○ ○

## Fibonacci example

```
struct Fibonacci {
  void operator()( int n, al::Shared w<int> result )
                                                    w->r
     if (n < 2) result.write( n );</pre>
                                                dependencies
     else {
        a1::Shared<int> subresult1;
        a1::Shared<int> subresult2;
        al::Fork<Fibonacci>()(n-1, subresult1);
        al::Fork<Fibonacci>()(n-2, subresult2)
        al::Fork<Sum>()(result, subresult1, subresult2);
struct Sum {
  void operator()( al::Shared w<int> result,
                    a1::Shared r<int> sr1,
                    a1::Shared r<int> sr2 )
  { result.write( sr1.read() + sr2.read() ); }
```

## Semantics & C++ Elision

```
struct Fibonacci {
  void operator()( int n, al::Shared w<int> result )
     if (n < 2) result.write( n );</pre>
     else {
        a1::Shared<int> subresult1;
        a1::Shared<int> subresult2;
        al::Fork<Fibonacci>()(n-1, subresult1);
        al::Fork<Fibonacci>()(n-2, subresult2);
        a1::Fork<Sum>()(result, subresult1, subresult2);
struct Sum {
  void operator()( al::Shared w<int> result,
                     a1::Shared r<int> sr1,
                     a1::Shared r<int> sr2 )
  { result.write( sr1.read() + sr2.read() ); }
```

## Semantics & C++ Elision

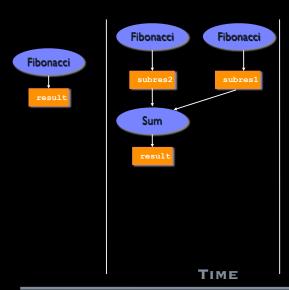
```
struct Fibonacci {
  void operator()( int n,
                                        int& result )
     if (n < 2) result =
     else {
                   int subresult1:
                   int subresult2;
                 Fibonacci ()(n-1, subresult1);
                 Fibonacci ()(n-2, subresult2);
                 Sum ()(result, subresult1, subresult2);
struct Sum {
  void operator()(
                                  int& result,
                               int srl,
                               int sr2 )
  { result =
                  sr1
                             + sr2
```

#### **Online construction**

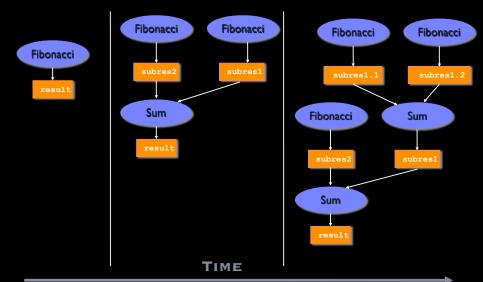


TIME

#### **Online construction**



#### Online construction



## Data Flow Graph Interests

- One abstract representation for
  - Scheduling
    - data flow graph ⇒ precedences graph ⇒ dependences graph
      - classical numerical kernel ⇒ partitioning the dependences graph
  - Explicit data transfer
    - data to be transferred is explicit in the data flow graph
      - automatic overlapping communication by computation
  - Original Fault Tolerant Protocols
    - TIC [IET05, Europar05, TDSC09]
      - coupling scheduling by work stealing with abstract representation
    - CCK [TSI07, MCO08]
      - coordinated checkpointing with partial restart after failure
  - Sabotage Tolerance [PDP09]
    - dynamically adapt the execution to sabotage
- Drawback: complexity to manage it

### Stack management

#### Stack based allocation

- Tasks and accesses to shared data are pushed in a stack
  - close to the management of the C function call stack
- O(1) allocation time
- O(#parameters) initialization time

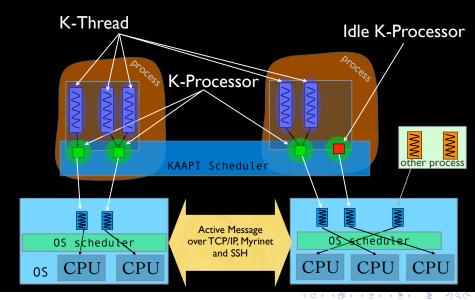
```
al::Shared<int> subresult1;
al::Shared<int> subresult2;
al::Fork<Fibonacci>()(n-1, subresult1);
al::Fork<Sibonacci>()(n-2, subresult2);
al::Fork<Sum>()(result, subresult1, subresult2);
```

Shared<int> sr1 Shared<int> sr1 Fibonacci, sr1 Fibonacci, sr2 Sum, r, sr1, sr2

### **Execution model**

- A (dynamic) set of UNIX processes
  - communication by active message
  - Each process is multithreaded
  - The root process forks the main task
- Threads inside processes are either
  - Performing work
    - excute tasks
  - idle and participate to scheduling
    - then it try to steal work (task) from other threads (work-stealing algorithm)

## 2 Level Scheduling

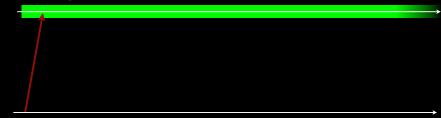


#### **Outline**

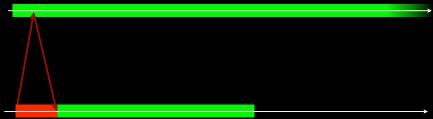
- Athapascan / Kaapi a software stack
- Foundation of work stealing
- Controls of the overheads

• Experiments with STL algorithms

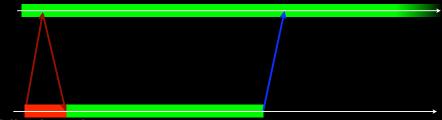
Working thread



Working thread



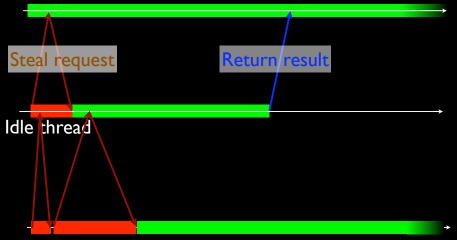
Working thread



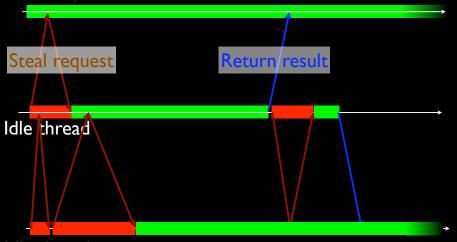
Working thread



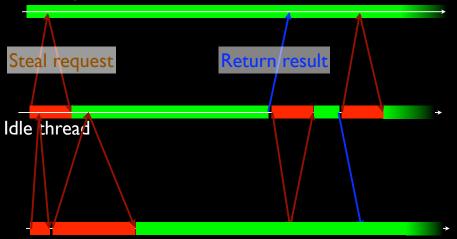
Working thread



Working thread



Working thread



## Work stealing queue

- Task: basic unit of computation
- Each thread has its own work queue

```
    push( task ) -> (): push a task
    pop() -> task : pop a task
```

- push / pop: LIFO order

used by the owner thread

- A idle thread can steal task from a victim thread's workqueue
  - steal() -> task : steal a task from the queue
  - push / steal: FIFO order

used by the thief thread

Random selection of victim threads

## **Assumption/Definitions**

- Fork/Join recursive parallel program
  - (formally: strict multithreaded computation)
- Notation:
  - T<sub>seq</sub>: "sequential work"
  - T<sub>1</sub>: execution time on 1 core of the parallel program, called "work"
  - T<sub>∞</sub>: time of execution on ∞ cores, called the "critical path" or the depth
  - T<sub>p</sub>: time of execution on P cores
  - P: the number of processors

#### Remarks

- $\bullet \ \mathsf{P}_{\infty} \stackrel{\mathsf{def}}{=} \mathsf{T}_1 \ / \ \mathsf{T}_{\infty}$ 
  - available parallelism (maximum speedup)
  - e.g. Fibonacci(30) = 83040
    - $T1 = 5.285*10^{-2}$ s,  $T_{\infty} = 3.08*10^{-7}$ s
    - **–**  $P_{\infty}$  ≈ 171591
- $\bullet$  T<sub>1</sub> / T<sub>seq</sub>
  - measure the work overhead
    - the creation of tasks
    - the work queue management (push/pop)

#### Theoretical bound

 Using work stealing scheduler with random selection of victim, the expected time on P processors is:

$$T_p = O(T_{seq} / P + T_{\infty})$$

 The expected number of steal requests per thread X<sub>D</sub> is:

$$X_p = O(T_\infty)$$

- [Blumofe, Leiseron, Focs 94, PPoPP 95], [Arora, Blumofe, Plaxton, SPAA 98], ...



## With data flow graph?

- Previous bounds: "fork/join" program
  - all created tasks are ready
- Not true in data flow program
  - complexity to compute data flow constraints
- Fortunately, the same bound holds
  - [Galilée, Doreille, Cavalheiro, Roch, PACT 98]
  - [Gautier, Roch, Wagner, ICCS2007]
    - in general case, the sequential execution is a valid execution
      - do not compute data flow constraints except on rare events



#### Remarks

#### Other interesting results

- Space efficient
- "Same" bounds for heterogenous machines (dynamic speeds) with slightly modified work stealing
  - [Bender, Rabin, SPAA00]

$$T_p = O(T_{seq} / (P \prod_{avrg}) + \beta T_{\infty} / \prod_{avrg})$$

- If P << P∞
  - $\rightarrow$  quasi linear speed up :  $T_p \sim c_1 T_{seq} / P$
  - Interest of fine grain parallel algorithm  $(T_{\infty} \ll T_1)$ 
    - $ightharpoonup P_{\infty} >> 1 !!$  allows wide range of quasi linear speedup

#### **Practical bound**

#### • Cilk 95

- $c_1$  ~ from 1 to 25, depends on the application
- **c**∞ ~ 1
- $T_p$  ≈  $c_1T_{seq}/p + c_\infty T_\infty$

#### Athapascan/Kaapi

- 1998:  $T_1/T_{seq} \sim 1$  10000: bad representation !
- 2004:  $T_1/T_{seq} \sim 1 1000$ : optimization
- 2006:  $T_1/T_{seq} \sim 1$  100: stack representation
- 2008:  $T_1/T_{\text{seq}} \sim 1$  20: + data flow constraints computed during steal operation



#### Related work

- Cilk [94, 95, 98]
  - one of the first language: 3 keywords cilk\_spawn, cilk\_sync, cilk\_for
  - sequential semantic !!!!
  - theoretical guaranteed performance
  - shared memory
- Tascell [09]
  - indolent closure creation (on demand)
  - distributed
  - using same idea as a Cilk extension [96] that has never been tested
- X10 [04, 08]
  - experimental language for HPC
  - extend class of parallel program with work stealing strategy
- Satin [01], Capsule [06]

#### Related work

- Cilk [94, 95, 98]
- Tascell [09]
- X10 [04, 08]
- Satin [01], Capsule [06]

- one of the first langue Athapascan/Kaapi [99, 03, 05, 07]
  - macro data flow: 2 keywords Fork, Shared
  - sequential semantic !!!!
  - theoretical guaranteed performance
  - shared & distributed memory
  - fault tolerant protocols
  - fine grain parallelism
    - Europar081
    - cooperative work stealing [09 Fr]

#### **Outline**

- Athapascan / Kaapi a software stack
- Foundation of work stealing
- Controls of the overheads

• Experiments with STL algorithms

## How to reduce T<sub>seq</sub>/T<sub>1</sub>?

- Why? => WORK overhead
  - extra instructions from the sequential program
  - especially for short computation (->STL algorithms)
- Three technics
  - adapt the grain size: stop parallelism after a threshold
    - but: increase  $T_{\infty}$ , reduce the average parallelism and increase the number of steal requests
    - difficulty to adjust it automatically
  - 2. reduce the cost to create task
    - ...ideally do not create task!
  - 3. optimize the cost of workqueue operations
    - difficulty due to concurrent operations



## How to reduce T<sub>seq</sub>/T<sub>1</sub>?

- Why? => WORK overhead
  - extra instructions from the sequential program
  - especially for short computation (->STL algorithms)
- Three technics
  - adapt the grain size: stop parallelism after a threshold
    - but: increase  $T_{\infty}$ , reduce the average parallelism and increase the number of steal requests
    - difficulty to adjust it automatically
  - 2. reduce the cost to create task
    - ...ideally do not create task!
  - 3. optimize the cost of workqueue operations
    - difficulty due to concurrent operations

• Cost = Creation + Extra arithmetic work

- Cost = Creation + Extra arithmetic work
- Example: prefix computation
  - input:  $\{a_i\}$ , i=0..n, output:  $p_i=\prod_{k=\{0..i\}} a_k$ ,  $\forall i=0..n$

- Cost = Creation + <u>Extra arithmetic work</u>
- Example: prefix computation
  - input:  $\{a_i\}$ , i=0...n, output:  $p_i = \prod_{k=\{0..i\}} a_k$ ,  $\forall i=0...n$
  - sequential work:

$$T_{seq}=n$$

- Cost = Creation + <u>Extra arithmetic work</u>
- Example: prefix computation
  - input:  $\{a_i\}$ , i=0...n, output:  $p_i = \prod_{k=\{0..i\}} a_k$ ,  $\forall i=0...n$
  - sequential work:

$$T_{seq}=n$$

- Parallel program => Ladner-Fisher (divide & conquer)  $T_{\infty} = 2 log_2 n, T_1 = 2 n$ 

- Cost = Creation + <u>Extra arithmetic work</u>
- Example: prefix computation
  - input:  $\{a_i\}$ , i=0..n, output:  $p_i=\prod_{k=\{0..i\}} a_k$ ,  $\forall i=0..n$
  - sequential work:

$$T_{seq}=n$$

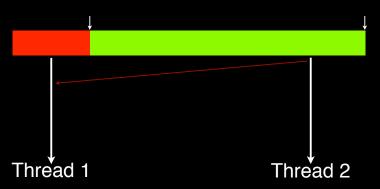
- Parallel program => Ladner-Fisher (divide & conquer)  $T_{\infty}=2 \log_2 n, T_1=2 n$
- Fish's lower bound: any parallel algorithm with critical path log<sub>2</sub> n requires at least 4n operations



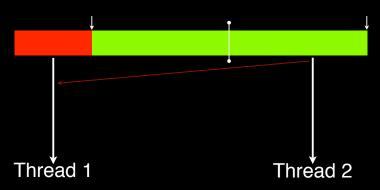
- [Roch, Traoré 07], [Roch, Traoré, Gautier 08]
  - Principe: create tasks when processors are idle!
- Task = apply  $F(a_i)$  for all elements  $a_i$  of an array



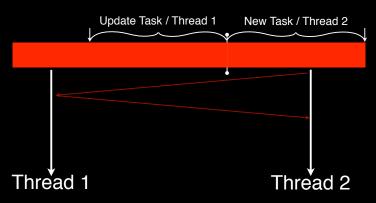
- [Roch, Traoré 07], [Roch, Traoré, Gautier 08]
  - Principe: create tasks when processors are idle!
- Task = apply  $F(a_i)$  for all elements  $a_i$  of an array



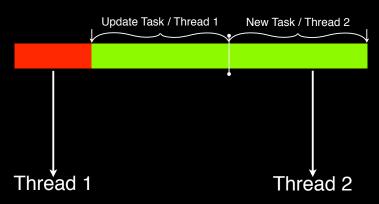
- [Roch, Traoré 07], [Roch, Traoré, Gautier 08]
  - Principe: create tasks when processors are idle!
- Task = apply  $F(a_i)$  for all elements  $a_i$  of an array



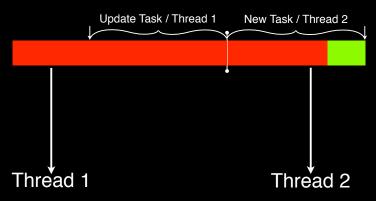
- [Roch, Traoré 07], [Roch, Traoré, Gautier 08]
  - Principe: create tasks when processors are idle!
- Task = apply  $F(a_i)$  for all elements  $a_i$  of an array



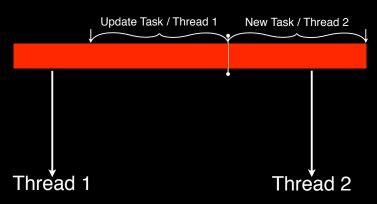
- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



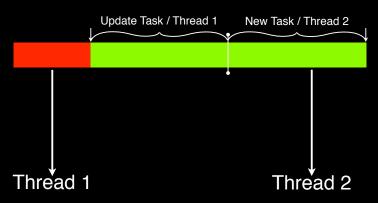
- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



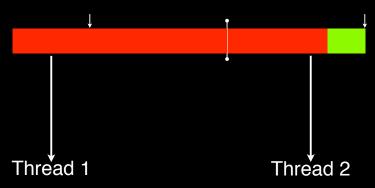
- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



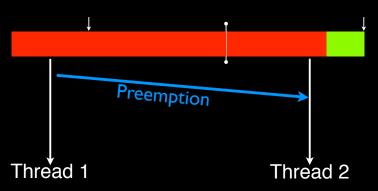
- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



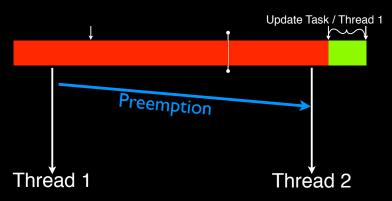
- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



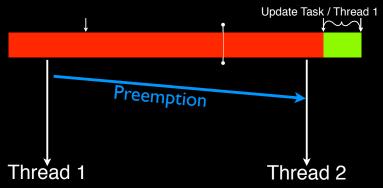
- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do



- Case of heterogeneous speed
  - Thread 2 is slower or as more work to do
  - We always use preemption: main thread (sequential algorithm) preempts thieves



### Algorithmic point of view

#### 2 Algorithms

- Sequential: efficiency
- Parallel: to split work & merge partial results

#### Scheduler

- interleaved execution of the two algorithms depending on the idle CPUs
- robust to heterogeneous processors

#### Workqueue optimization

- 3 operations
  - push / pop / steal
- Algorithms
  - Cilk: T.H.E. protocol
    - serialization of thieves to a same victim
    - thief/victim atomic read/write + lock in rare case
  - ABP [SPAA00]:
    - lock free (Compare&Swap), but prone to overflow
  - Chase & Lev [SPAA05]:
    - without limitation (other than hardware)
- → COSTLY 'cas' operation [PPoPP09]

#### Role of the 'CAS'

- Consensus between N-thieves and the victim
  - In theory, not possible (if wait free) with less powerful synchronization primitive
  - e.g.: atomic register read/write, test&set
- How to avoid 'CAS' ?

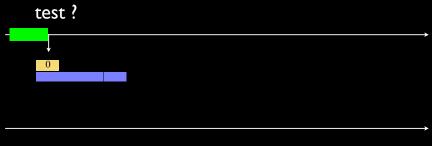
#### Relaxed semantics

- "Idempotent work stealing" [PPoPP09]
  - Maged M. Michael, Martin T. Vechev,
  - Vijay A. Saraswat (work also on X10 language)
  - avoid CAS in pop operation
- <u>→ More Performance</u>
- Drawback
  - a task is returned (and executed) at least once
  - ... instead of exactly once

## Cooperative approach

- [X. Besseron, C. Laferrière]
- Keep same semantics as usual
  - a task is extracted exactly once
- so...avoid concurrency between victim & thieves
  - the victim interrupts its work to process steal requests
  - some similarity with TasCell [09], Capsule [06]
- Drawback
  - the victim should poll requests
  - thieves are waiting



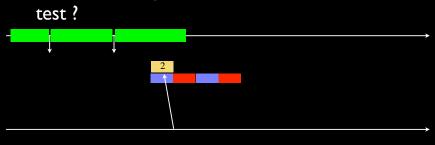


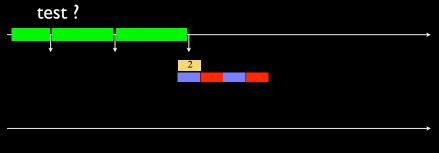


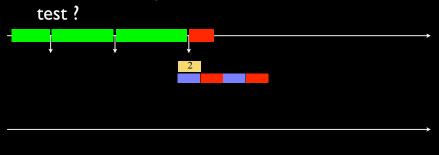


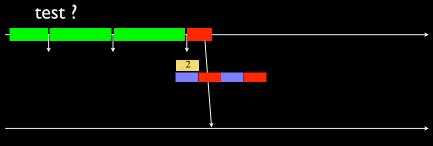


test ?

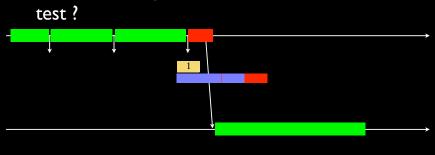


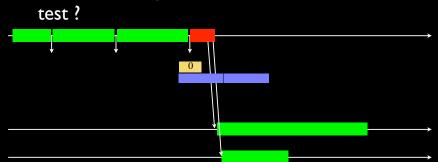


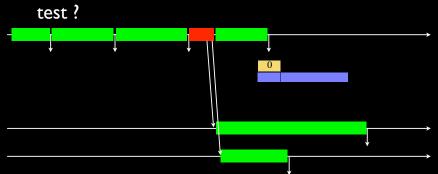


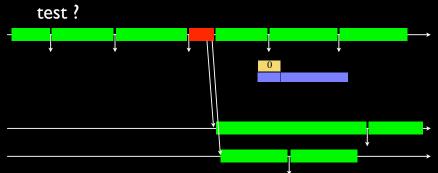


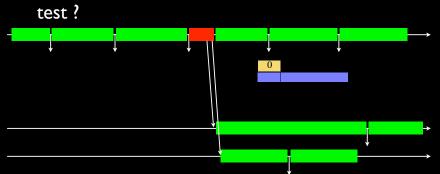
test ?



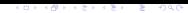








- Gain
  - work overhead: 1 read on memory
  - reply to K thieves in place of only 1
    - better workload balance



### **Outline**

- Athapascan / Kaapi a software stack
- Foundation of work stealing
- Controls of the overheads

Experiments with STL algorithms

#### **KaSTL: Parallel STL**

- [PhD Daouda Traoré, 2008]
- Technics applied to 95% of STL algorithms
  - STL: Standard C++ Template Library
- Comparison with other library
  - Cilk++, Intel Thread Building Block (TBB)
  - MCSTL (GNU STL parallelized with OpenMP)
- Multiprocessor: 8 AMD CPUs with 2 cores

## **Experiments**

#### Two set of experiments

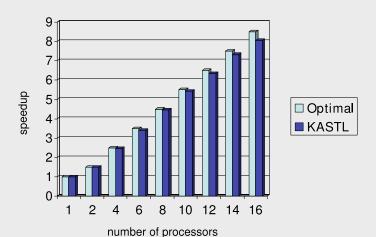
- 1/ with adaptive algorithms
  - PhD of [Daouda Traoré]
- 2/ with cooperative work stealing
  - [Daouda Traoré, Xavier Besseron, Christophe Laferrière]

#### Methodology

- average over 30 runs
- 1 run = average of 100 basic experiments, do not take into account the first experiment

### **Prefix**

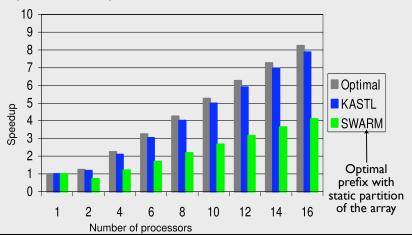
- Homogeneous processors
   \* coarse grain, 30000 elements



### **Prefix**

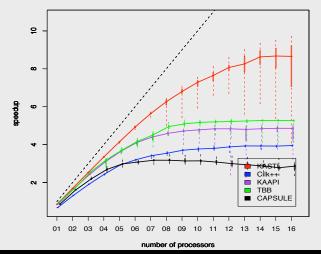
#### Heterogenous

- (p-1) processors have the same speed S
- 1 processor has speed S/2



### Sort

• ~ 100M elements, 1s sequential time sort - medium size (~1s) - speedup

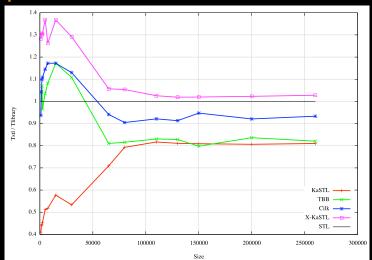


### **Partial conclusion**

- Interest to adapt the task to activity (or idleness) of processors
- But coarse computation
  - sequential time > 0.1s
- + Cooperative work stealing
  - named X-KaSTL or CKaapi in diagrams

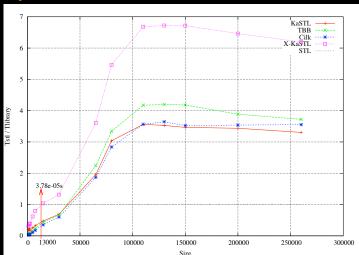
#### std::transform

#### • 1 processor



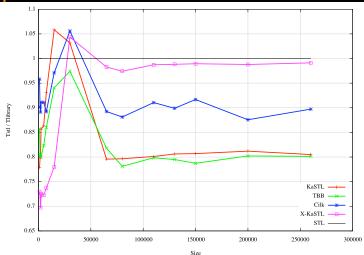
#### std::transform

• 8 processors NUMA machine



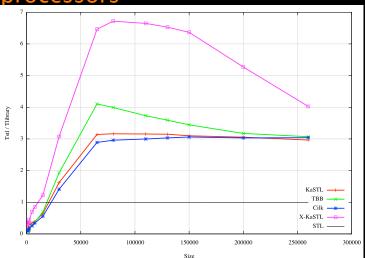
### std::merge

• 1 processor



### std::merge

8 processors

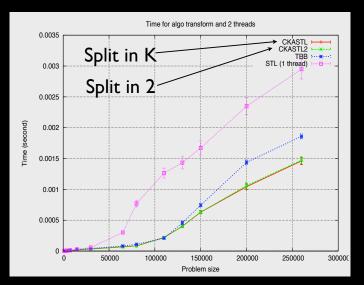


#### **Partial conclusion**

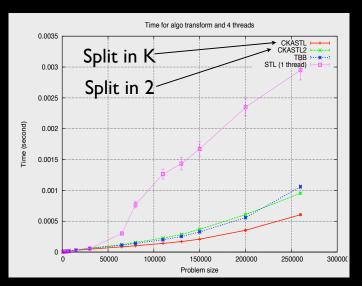
- Effective speedup at finer computation
  - sequential time  $\sim 10^{-3}$ s = 1ms

- impact of the better balance of work load
  - comparison split in K versus split in 2

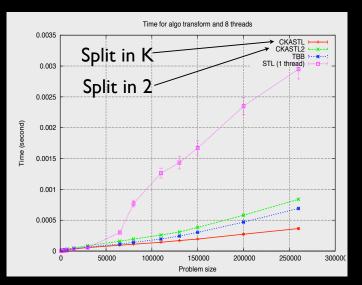
### "Transform" 2 threads



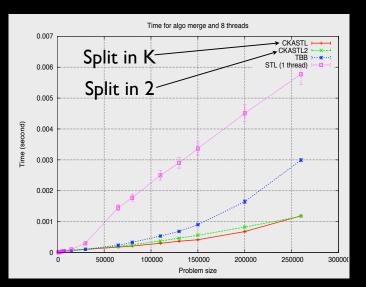
### "Transform" 4 threads



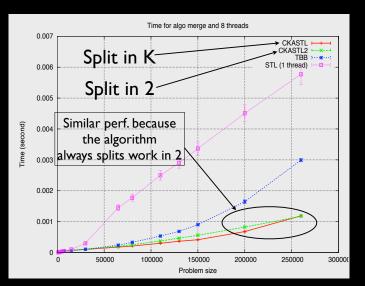
### "Transform" 8 threads



# "Merge", 8 threads



## "Merge", 8 threads



#### Conclusion

- Athapascan/Kaapi
  - a data flow model with lazy task generation
    - reduce the work overhead
  - sequential semantics
  - original approach
  - effective parallelization of fine computation
    - with cooperative workstealing
- http://kaapi.gforge.inria.fr/
- Drawback
  - non standard research software
    - difficulty to port already parallelized applications

## **Perspectives**

- Software being to be more robust
  - INRIA action to support development (2 years)
  - Ported on top of most Unix (Linux, MacOSX, [SunOS], iPhoneOS]
  - [2010] will be ported on IBM/BlueGene
  - [2010] will be ported on MPSoC with ST Microelectronics
- Viability of the cooperative approach
  - not yet theoretical fundation
  - coupling technics with concurrent work stealing

## **Perspectives**

- Mixing CPUs & GPUs
  - preliminary work
  - deeper integration of the GPU as a processing resource
     next Fermi GPU + driver?
- Better coupling between OS & Middleware
  - importance to know (in advance) the available number of resources
- Taking into account NUMA architecture
  - ongoing work at MOAIS [JN Quintin, PhD]

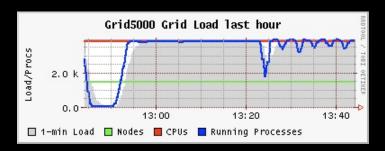
## Other applications

- [Parallelization of Bayesian computation]
- Parallel Computer Algebra
  - Linbox: http://www.linalg.org
- Combinatorial Opt. [PRiSM (Paris), B. Lecun]
- Academic applications
  - [III, IV, V Grid@Work contest]
    - NOueens
    - Option Pricing application based on Monte Carlo Simulation
  - Numerical kernel for CEM, CFD Grid application
    - Finite difference / Finite element
  - Reaction / diffusion with Chemical species
    - Finite difference
- SOFA (<a href="http://www-sofa-framework.org">http://www-sofa-framework.org</a>)





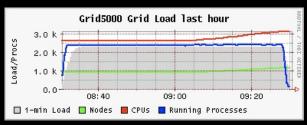
### **NQueens** [2006,2007]



- Grid5000 (French academic national grid)
  - 2006: N=23 in 74min on 1422 cores
  - 2007: N=23 in 35mn 7s on 3654 cores
- Taktuk: fast deployment tool



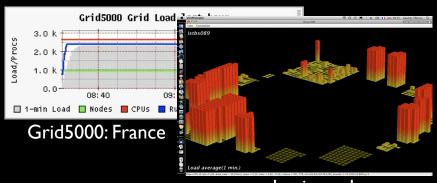
#### Monte Carlo / Option Pricing



Grid5000: France

- 3609 cores: ~2700 Grid5000 ~900 Intrigger
- SSH connection between Japan–France

#### Monte Carlo / Option Pricing



- Intrigger: Japan
- 3609 cores: ~2700 Grid5000 ~900 Intrigger
- SSH connection between Japan–France



- SOFA: real-time physics engine
- Strongly supported INRIA initiative
- Open Source: <a href="http://www.sofa-framework.org">http://www.sofa-framework.org</a>
- Target application:Surgery simulation

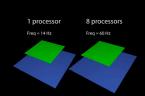


## Physics Simulation

- SOFA: real-time physics engine
- Strongly supported INRIA initiative
- Open Source:

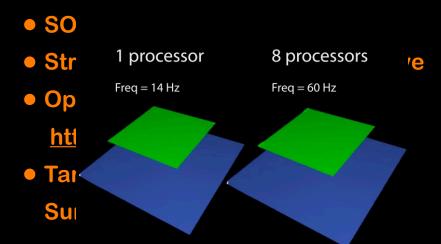
http://www.sofa-framework.org

Target application: **Surgery simulation** 



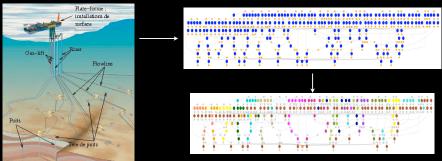


# **Physics Simulation**



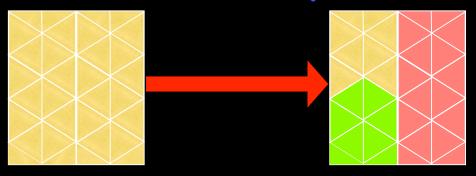
#### **Iterative Application**

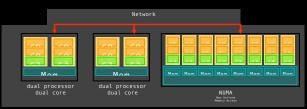
- Scheduling by graph partitioning
  - Metis / Scotch



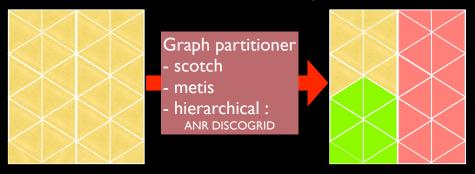
**Application** 

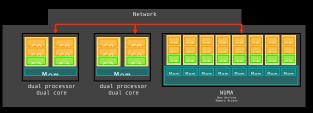
#### **Domain decomposition**





#### **Domain decomposition**





#### **Experiments**

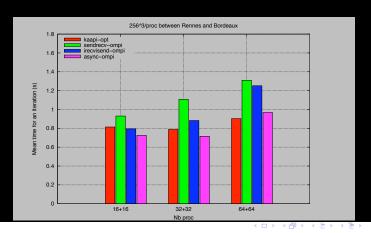
#### Finite Difference Kernel

- Kaapi / C++ code versus Fortran MPI code
- Constant size sub domain D per processor
- Cluster: N processors on a cluster
- Grid: N/4 processors per cluster, 4 clusters

D=256^3	# processors	Cluster (s)	Grid (s)	Overhead
KAAPI		0.49	0.49	-
	64	0.55	0.84	0,53
	128	0.65	0.91	0,4
MPI		0.44	0.44	-
	64	0.66	2.02	2,06
	128	0.68	1.57	1,31

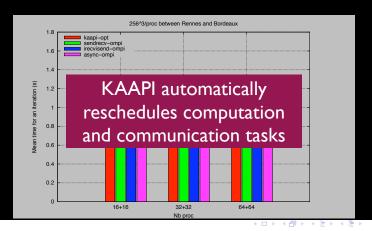
### Optimizing MPI code

- Overlapping communication by computation
  - At the cost of important code restructuring



### Optimizing MPI code

- Overlapping communication by computation
  - At the cost of important code restructuring



#### Communication

- Active message like communication protocol
- Multi-network (TCP, Myrinet, ssh tunnel with TakTuk)
- High capacity to overlap communication by computations
- Original message aggregation protocol



