

# ENERGY STORAGE AND REAL-TIME GENERATION SCHEDULING

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joint work with

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# Outline

1. Introduction and motivation
2. Socially optimal scheduling of generation and storage
3. Real-time Market efficiency and distributed control

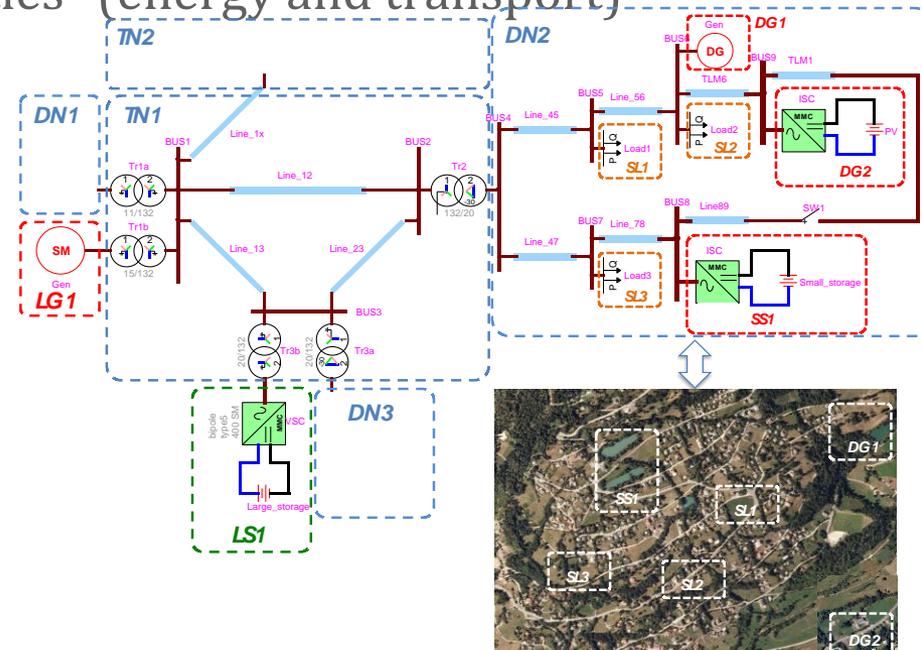
# Storage and Demand Response can be used to mitigate volatility of renewables

## ■ Motivation:

- ▶ Swiss Nanotera  $S^3$  grid (M. Kayal, M. Paolone) use of storage in active distribution network
- ▶ European FP7: Quanticol: Quantitative methods for collective adaptive systems. Applications in “smart cities” (energy and transport)

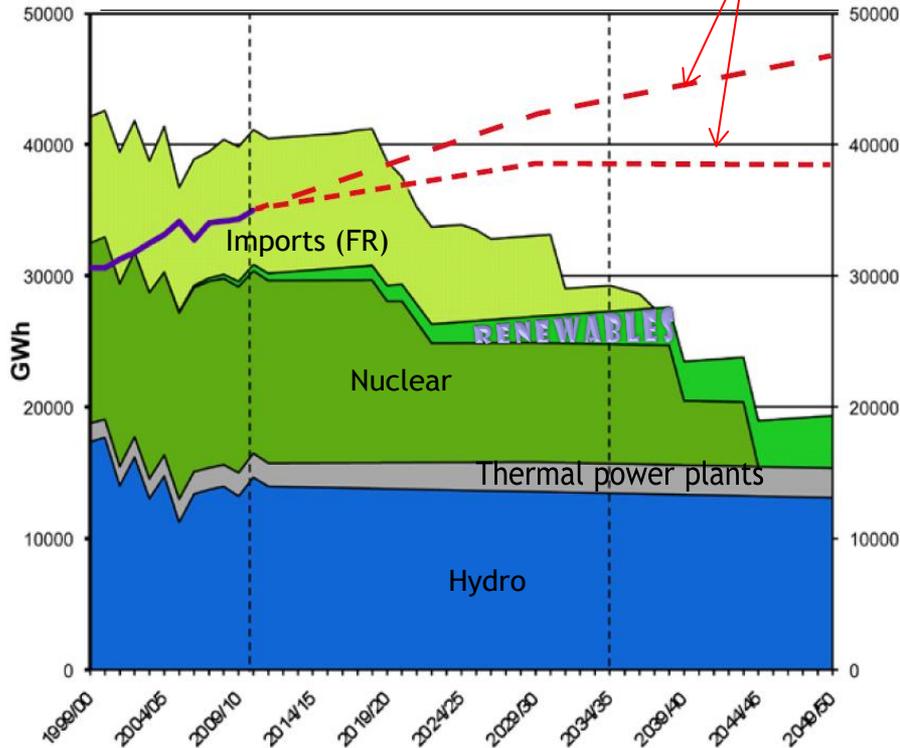
## ■ In this talk:

1. can we use storage to compensate for renewable forecast errors ?
2. can we control storage with prices ?



# Motivation: energy transition

Forecasted demand (two scenarios)



Planned swiss annual electricity production

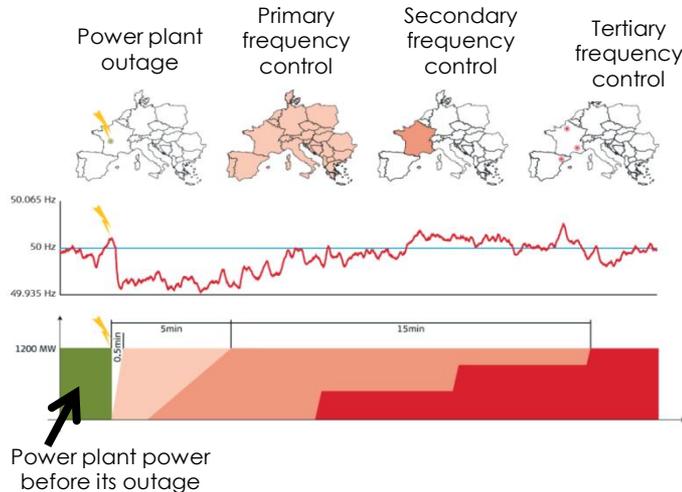
Switzerland plans to shut down nuclear power plants by 2030-2050

- Current options
  - Reduce consumption
    - Problem: population growth
  - Gas, coal, oil
    - Pollution
    - Empowers owners of resource
  - Renewables
    - Clean!
    - Slow (expensive?) deployment
    - **Volatile: need for storage!**

# Real-time control problem

## 1. Energy Balance and Frequency control

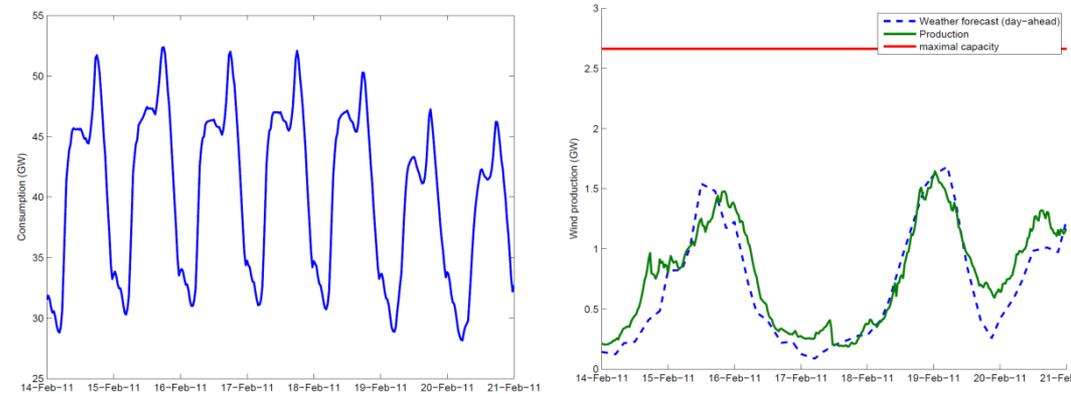
- ▶ Conventional generators have delays
- ▶ A fixed “reserve” has to be available (**deterministic**, empirically decided).



## 2. Voltage control

(distribution network, will not be discussed today)

- Demand is predictable
- Renewables are not



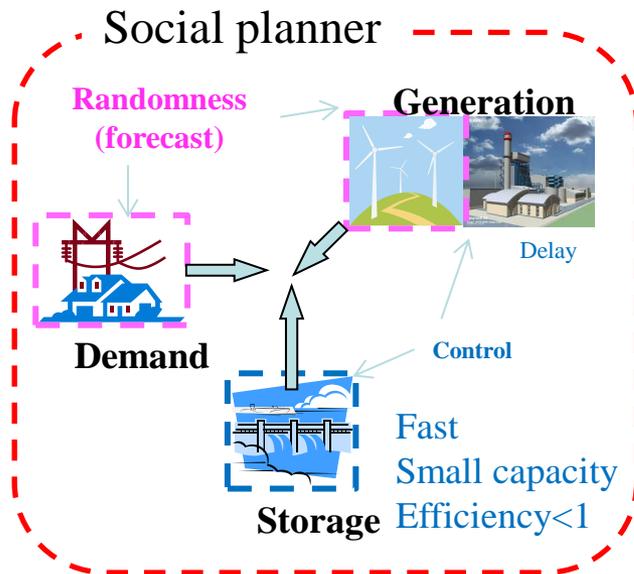
Example: national data from the UK

- Deterministic approach
  - ▶ Large security margin / reliability
- Stochastic optimization
  - ▶ NP-hard problem or worse
- Solution: approximate solutions
  - ▶ Approximate dynamic programming

# Two topics in this talk

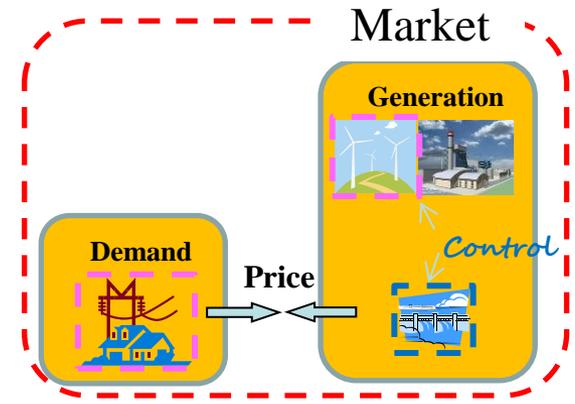
## ■ Socially optimal scheduling of generation and storage

- ▶ Use of storage to compensate for forecast uncertainties



## ■ Market efficiency

- ▶ Is there a price such that Consumer and Producer agree?
- ▶ Will it lead to a socially optimal use of resources (or losses due to over-cycle of storage)?
- ▶ Consequences on investment?



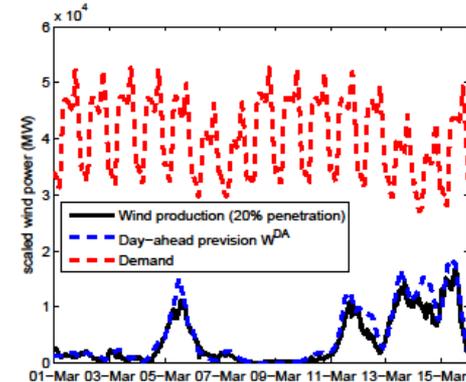
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# Production scheduling w. forecasts errors

## ■ Base load production scheduling

- ▶ Deviations from forecast
- ▶ Use storage to compensate



## ■ Compare two approaches

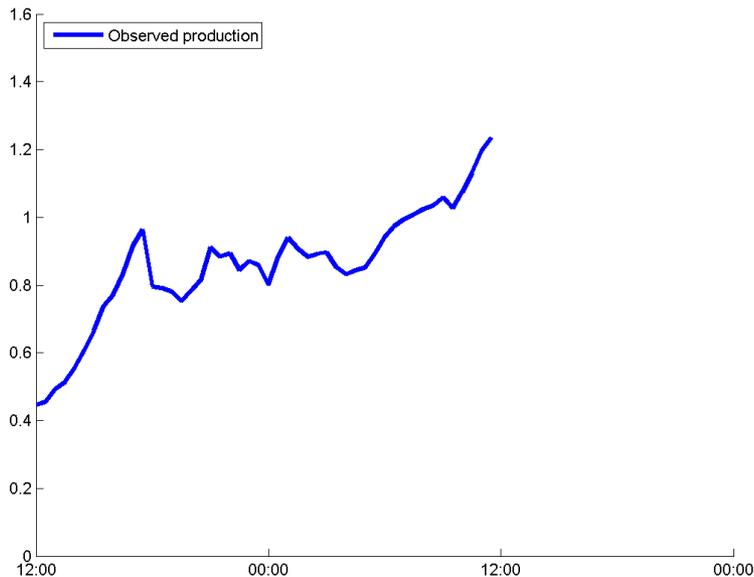
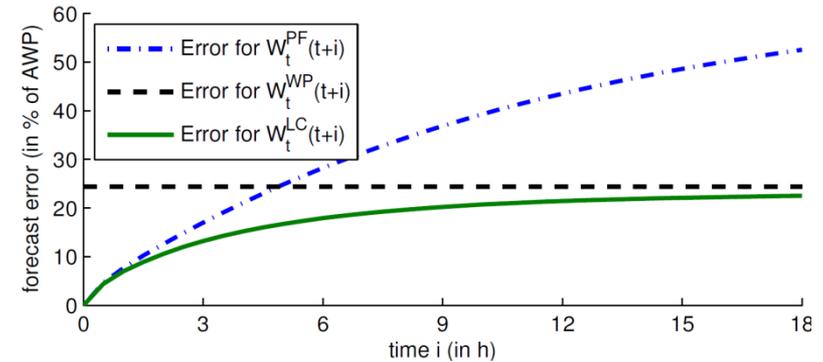
1. Deterministic approach (model predictive control, rolling horizon, ...)
  - ▶ try to maintain storage level at e.g.  $\frac{1}{2}$  of its capacity using updated forecasts
2. Stochastic approach
  - ▶ Use statistics of past errors.



Pump hydro, Cycle efficiency  $\approx 80\%$

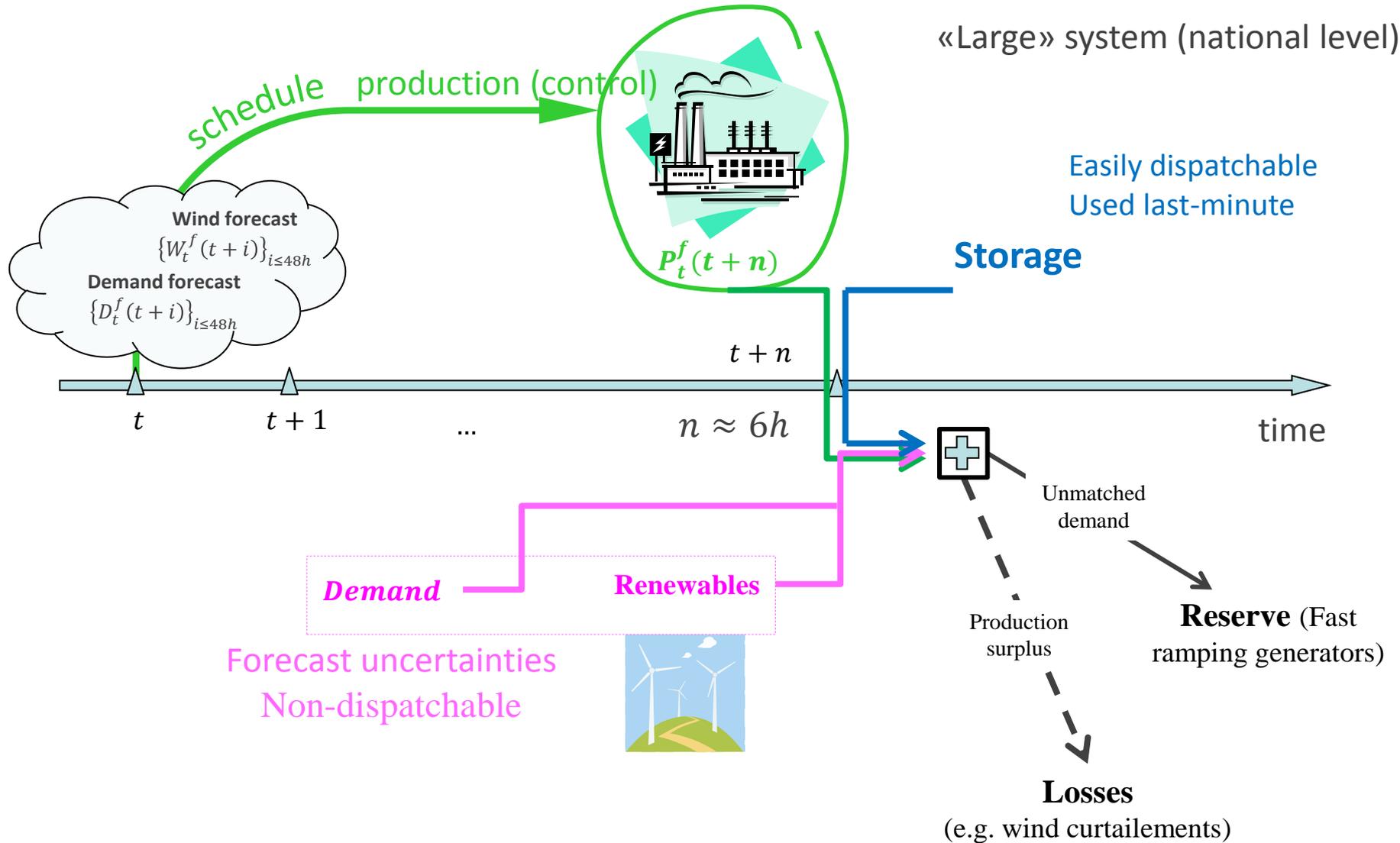
# Wind forecasting errors

- At time  $t$ , we are given a forecast of future production or demand
- We schedule the “baseload production” using this forecast



- Social planner point of view
  - ▶ Quantify the benefit of storage
  - ▶ Obtain performance baseline
    - ▶ what could be achieved
    - ▶ no market aspects
- Given a forecast, what can be achieved?

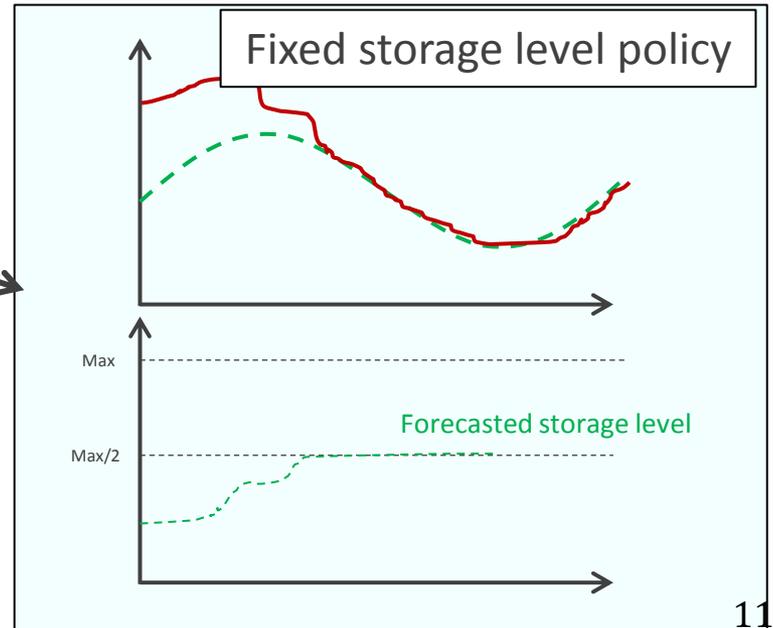
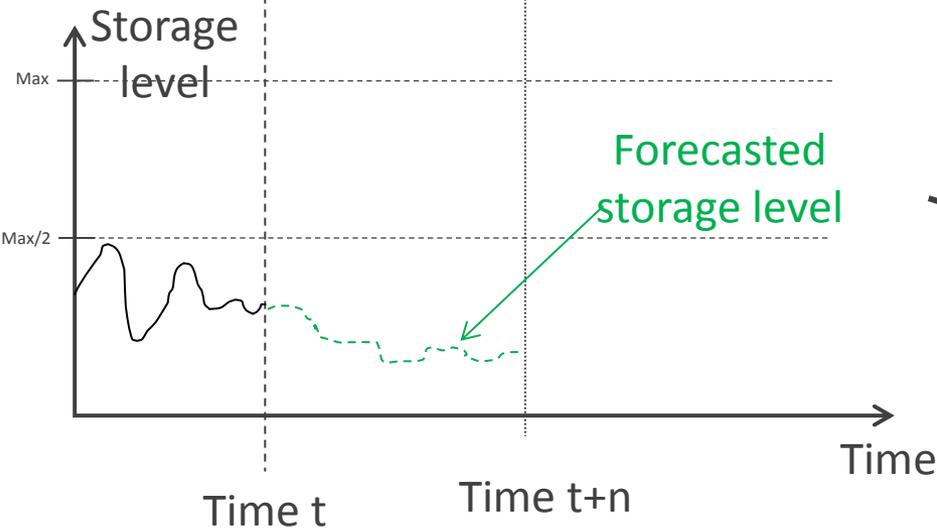
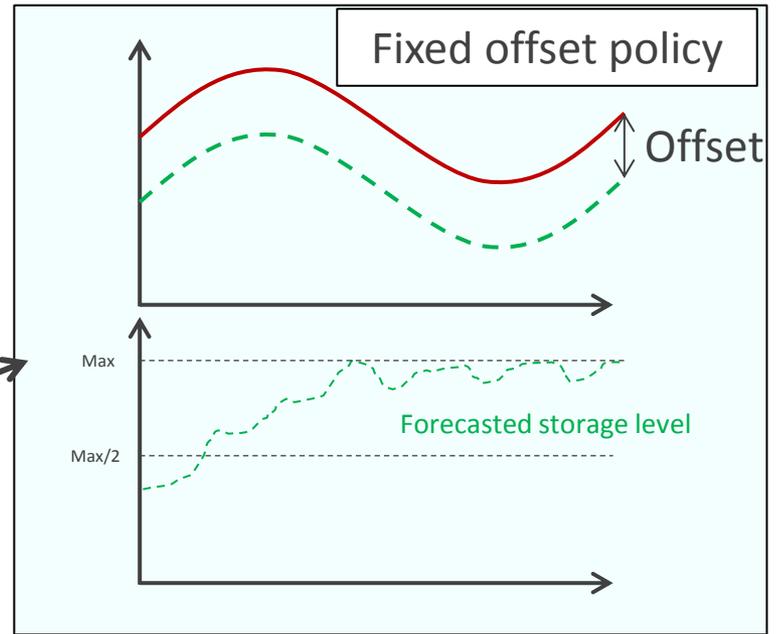
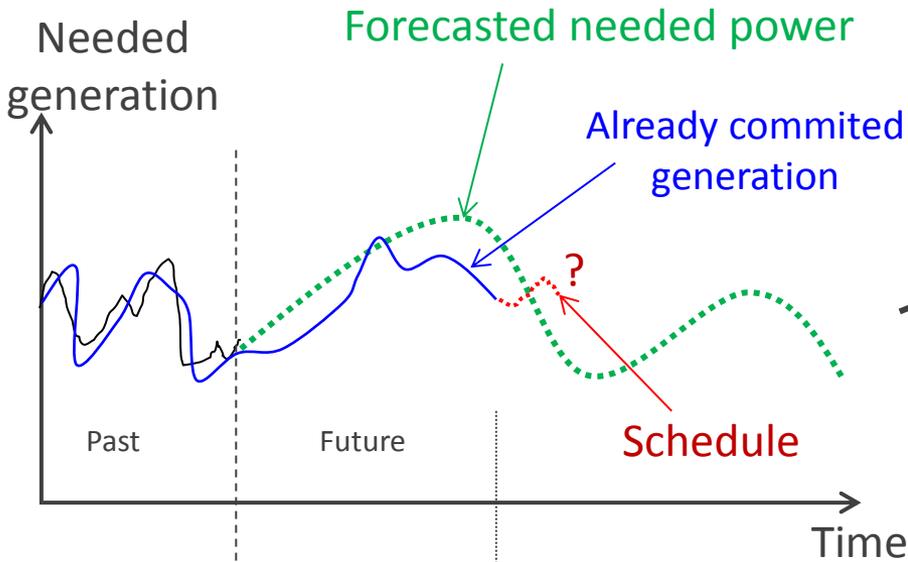
# Energy scheduling with delays



**Difficulty:** Markov decision processes with delays

- Optimal control problem intractable

# Example of scheduling heuristics

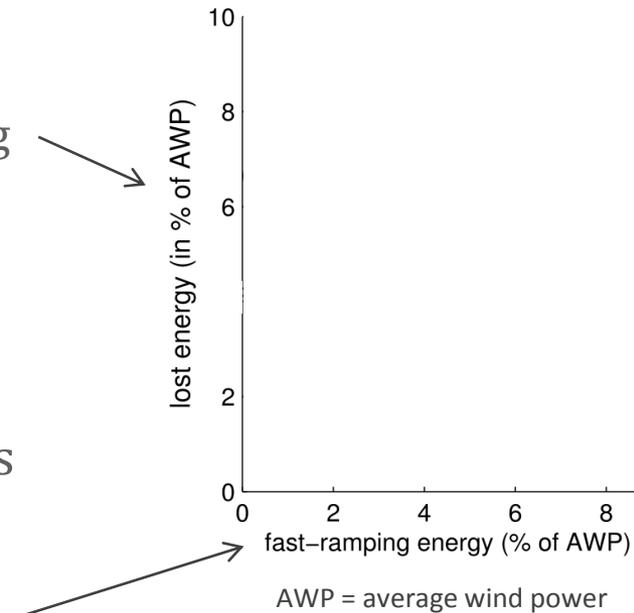


# Metric and performance (large storage)

## ■ Energy may be **wasted** when

- ▶ Storage is full
- ▶ Unnecessary storage (cycling efficiency < 100%)

## ■ **Fast ramping energy** sources ( $CO_2$ rich) is used when storage is not enough to compensate fluctuation



Numerical evaluation: data from the UK  
(BMRA data archive <https://www.elexonportal.co.uk/>)

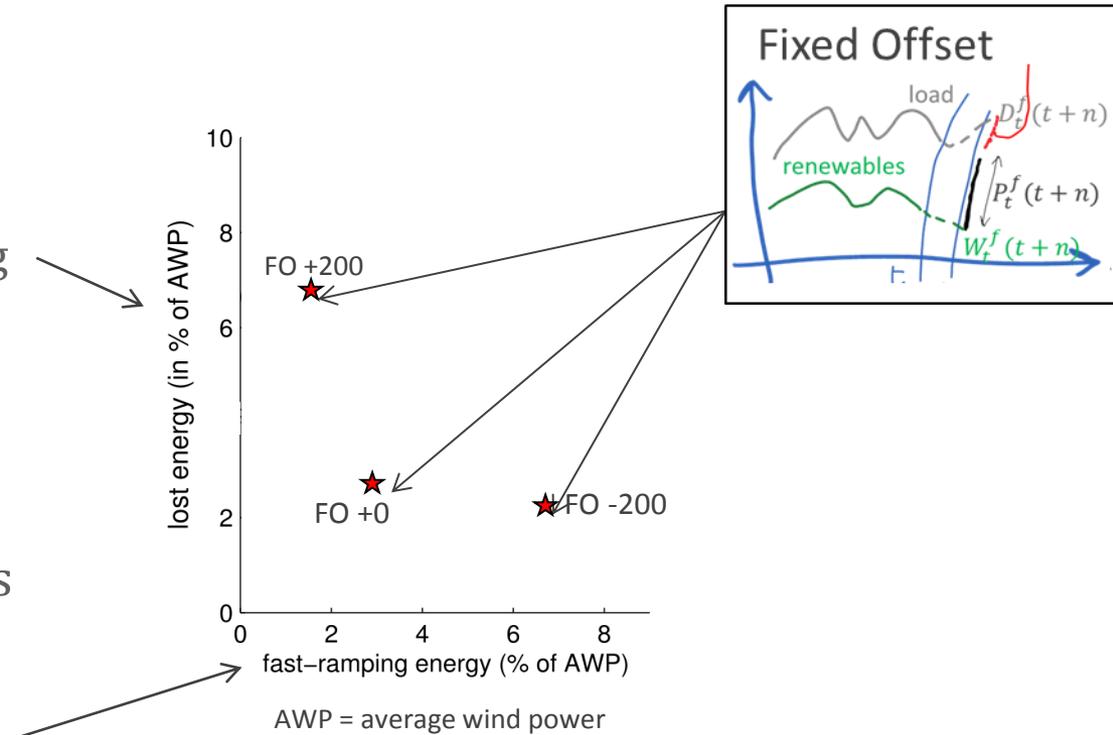
- National data (wind prod & demand)
- 3 years
- Corrected day ahead forecast: MAE = 19%

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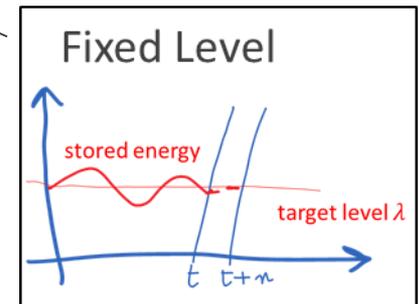
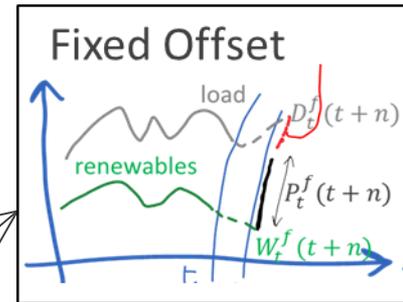
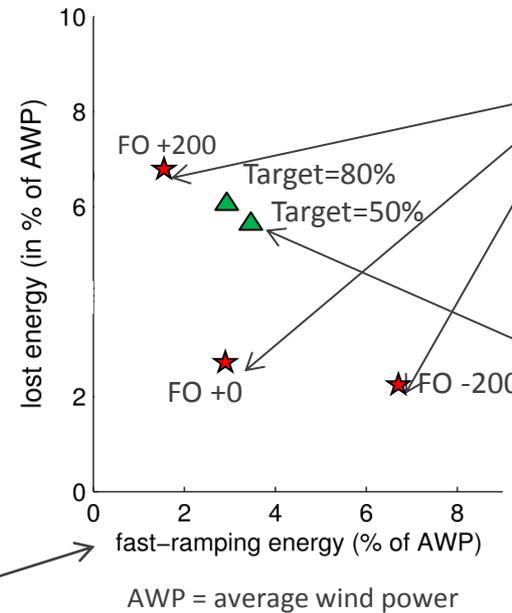
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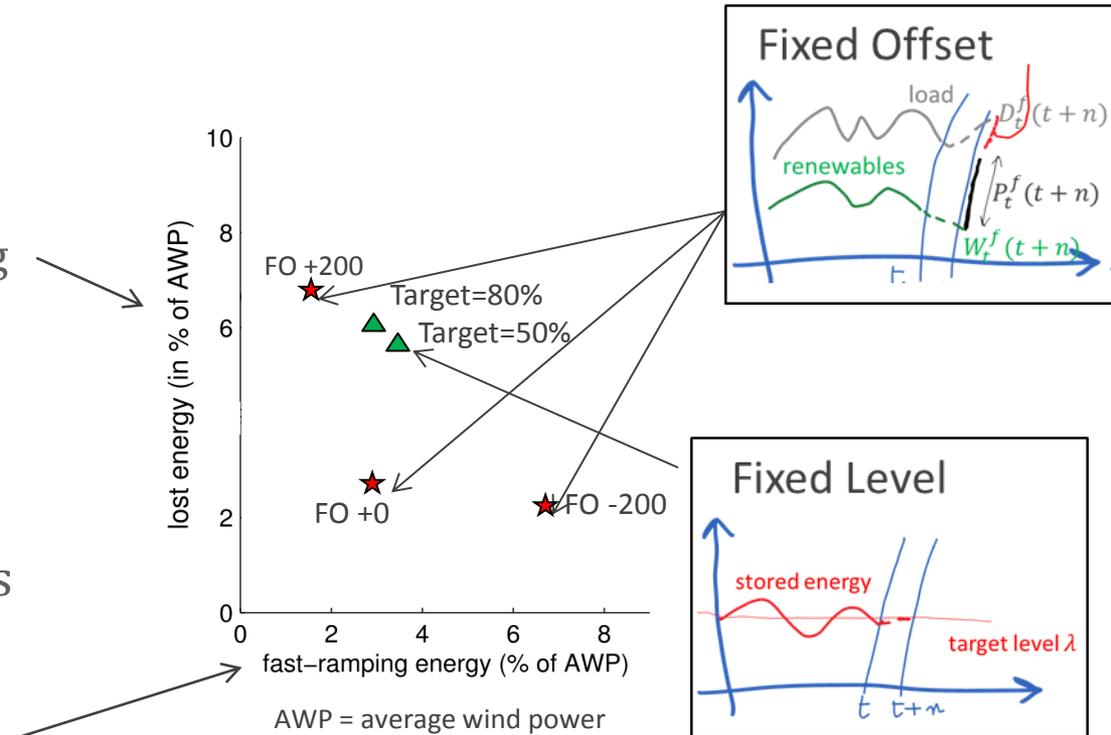
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- National data (wind prod & demand)
- 3 years
- Corrected day ahead forecast: MAE = 19%

## Questions:

- Can we do better?
- How to compute optimal offset?

# Fixed offset is optimal for large storage

Let  $\ell(u) := \mathbb{E}[(\varepsilon+u)^+] - f(u)$  with  $f(u) := \min(\eta \mathbb{E}[\min((\varepsilon+u)^+, C_{\max})], \mathbb{E}[\min((\varepsilon+u)^-, D_{\max})])$   
 $g(u) := \mathbb{E}[(\varepsilon+u)^-] - f(u)$

**Theorem.** If the forecast error is distributed as  $\varepsilon$  Then:

1.  $(\ell, g)$  is a **lower bound**: for any policy  $\pi$ , there exists  $u$  such that:

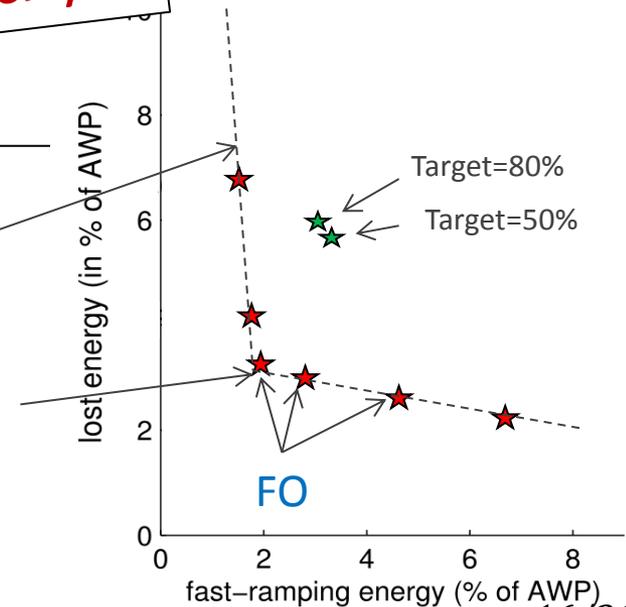
$$\bar{G}^\pi(T) \geq g(u) - \frac{B_{\max}}{T} \quad \bar{L}^\pi(T) \geq \ell(u) - \frac{B_{\max}}{T}$$

2. **FO is optimal for large storage**: if  $B_{\max} \gg B_\delta$ , then

3. The **Problem solved for large capacity**  
  - What about small / medium capacity?

- Uses distribution of error
- Fixed reserve is **Pareto-optimal**

$(\ell, g)$  curve :  
Lower bound  
Optimal fixed offset  
 $u = 2\%$  AWP



# Scheduling Policies for Small Storage

## ■ Dynamic offset policy:

- ▶ choose offset as a function of forecasted storage level

## ■ Stochastic optimal control (general idea)

- ▶ Compute a value  $V(B)$  of being at storage level  $B$

$$u = \underset{u \in \text{offset}}{\operatorname{arg\,inf}} \mathbb{E}[\text{cost}(u) + V(\phi(b, u))]$$

Expectation on possible errors      Instant cost (losses or fast-ramping energy)      Storage level at next time-slot

## ■ Computation of $V$ : depends on problem

- ▶ Here: solution of a fixed point equation:

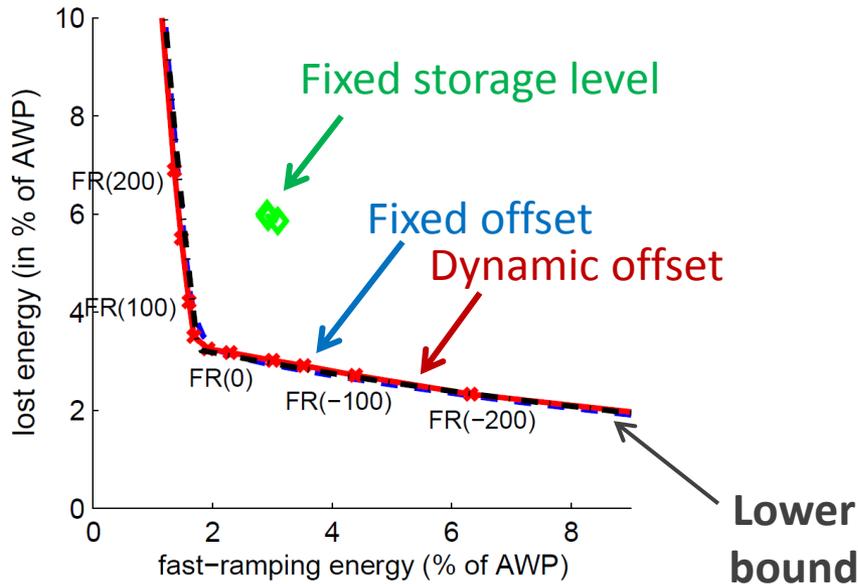
$$V(b) = g + \underset{u \in \text{offset}}{\operatorname{inf}} \mathbb{E}[\text{cost}(u) + V(\phi(b, u))]$$

- ▶ Approximate dynamic programming if state space is too large
- ▶ Can be extended to more complicated state  $V(t, B, B', \dots)$

# Dynamic Offset outperforms other heuristics

## Large storage capacity (=20h of average production of wind energy)

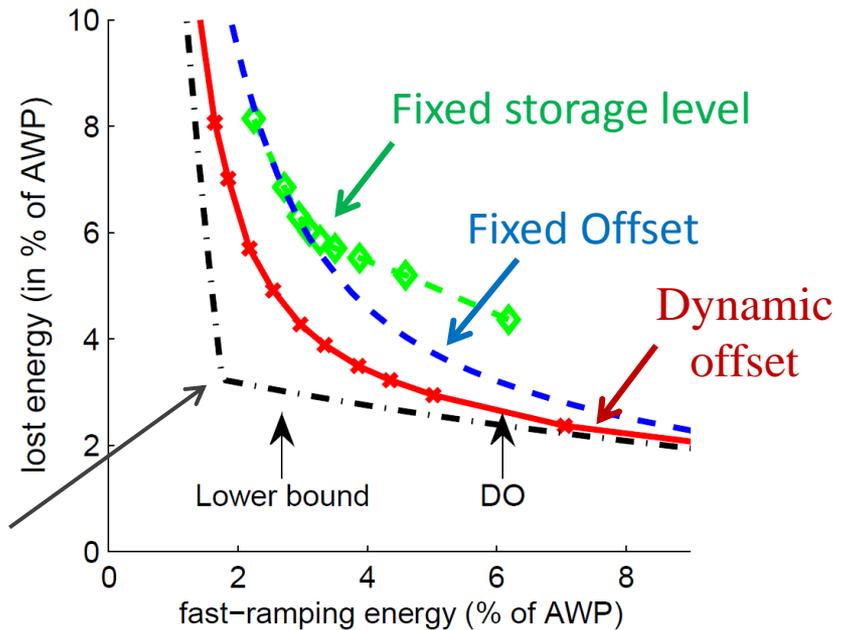
- ▶ Power = 30% of average wind power



- ▶ Fixed Offset & Dynamic offset are optimal

## Small storage capacity (=3h of average production of wind energy)

- ▶ Power = 30% of average wind power



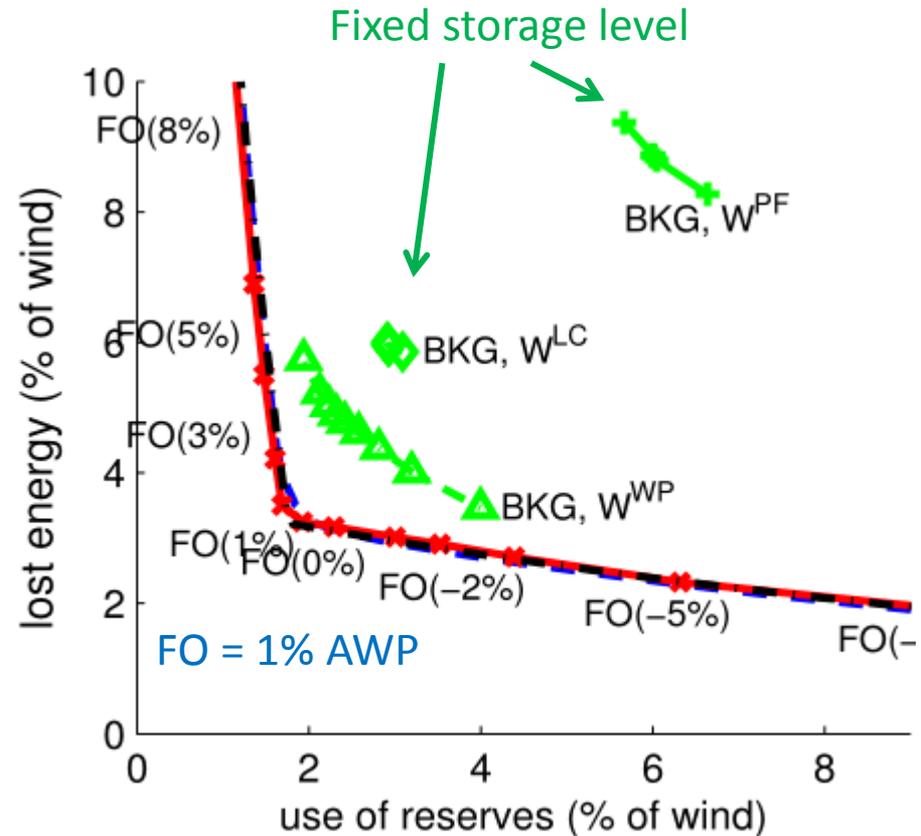
- ▶ DO is the best heuristic

Maintaining storage at **fixed level: not optimal**

There exist better heuristics

# Take Home Message

- For “large” (i.e. one day) storage, there is an optimal value of fixed offset reserve, which can be computed from forecast error statistics
- Can be used to dimension secondary reserve

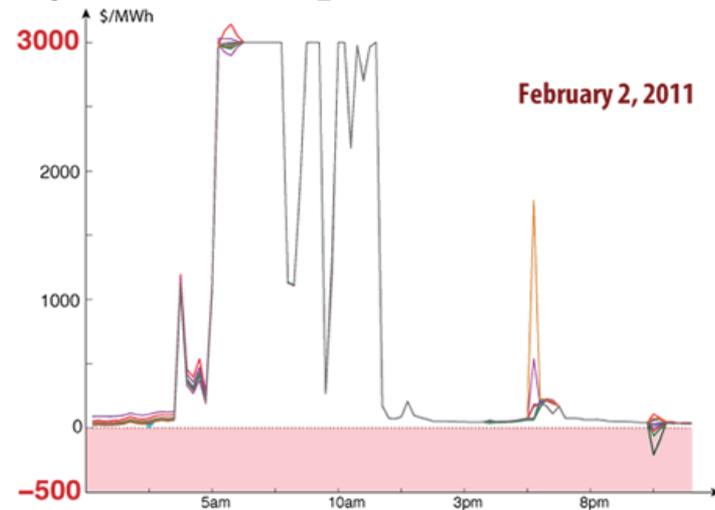
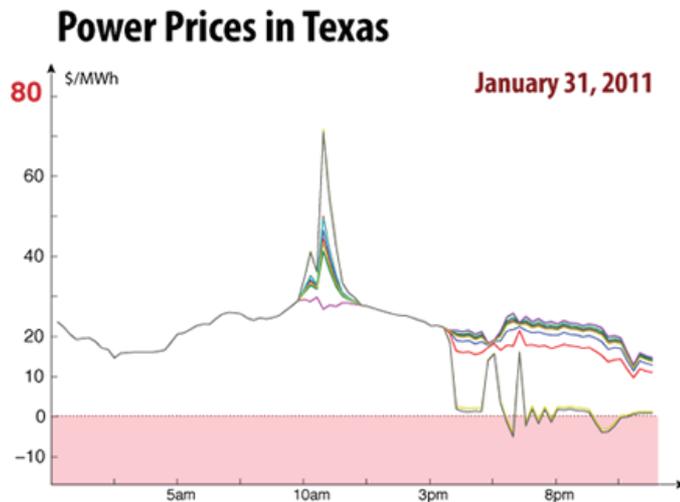


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# Real-time Market

- US Electricity markets are organized in two stages
  - ▶ Day-ahead (On-peak / off-peak)
  - ▶ Real-time (deviations from forecast)
- Europe wants to do the same
- Real-time markets exhibit highly volatile prices



- Efficiency or Market manipulation?

# The first welfare theorem

- Impact of volatility on prices in real time market is studied by Meyn and co-authors: price volatility is expected

**Theorem** (Cho and Meyn 2010). When dynamics (generation constraints) are taken into account:

- Markets are efficient
- Prices are never equal to marginal production costs.

- Efficiency or Market manipulation? : hard to distinguish

We add storage to the model

- Q1: Market implies socially optimal control (efficiency)?

- ▶ Is there a price that dictates both generation scheduling and storage usage? (even when cycle efficiency  $< 100\%$ ?)

- Q2: what are the effects on prices?

- Q3: does it lead to socially optimal investments strategies?

# A Macroscopic Model of Real Time Market with Storage

H:  $(D - \Gamma) \sim$  brownian motion

Randomness



**Demand**

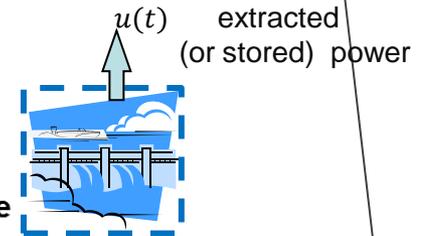
$$D^a(t) = d^{da}(t) + D(t)$$



**Supply**

$$G^a(t) = g^{da}(t) + G(t) + \Gamma(t)$$

Day-ahead



**Storage**

$$\frac{\partial B}{\partial t} = -u(t)(1_{u(t)>0} + \eta 1_{u(t)<0})$$

$u(t)$  extracted (or stored) power

Control

Ramping Constraint

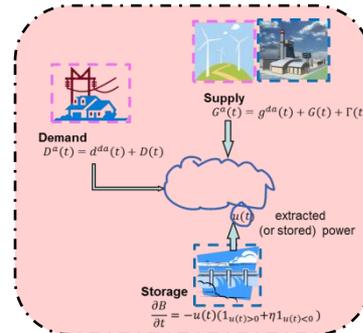
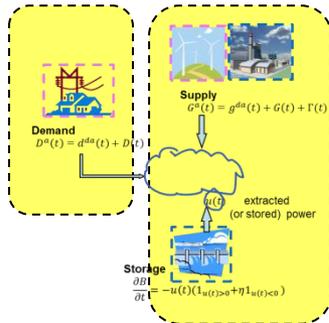
$$-\xi \leq G(t) - G(t-1) \leq \zeta$$

Storage cycle efficiency

(E.g.  $\eta = 0.8$ )

Limited capacity

## Questions:

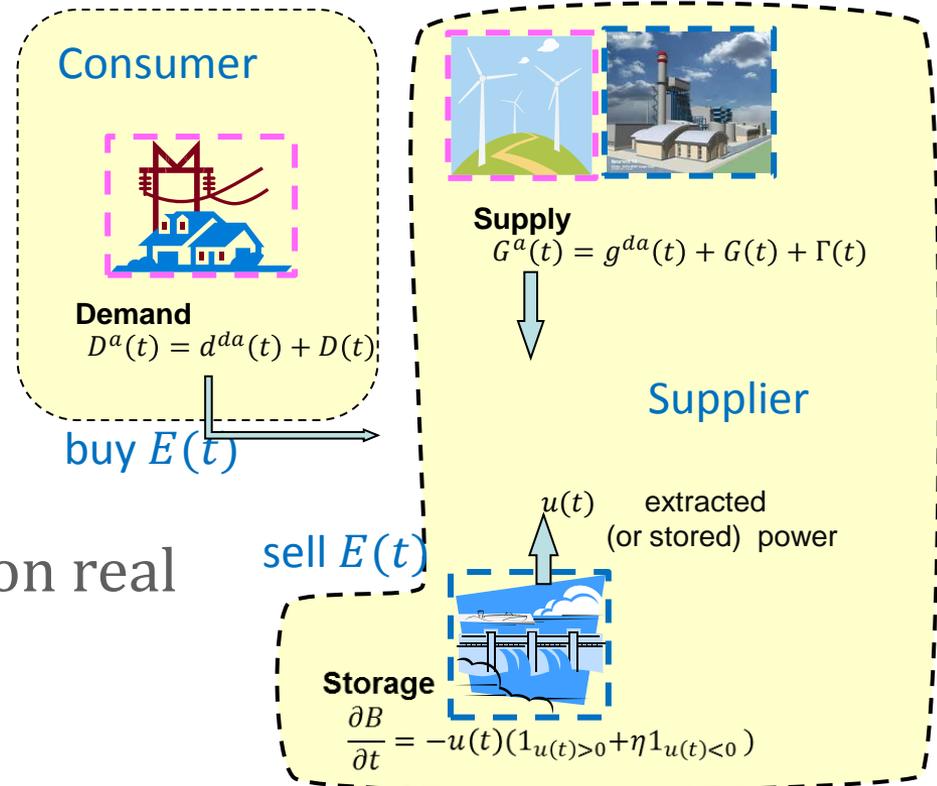


1. Competitive equilibria: definition and existence.

2. Relation to social planner's problem

# Scenario A: Storage at Supplier

$P(t)$  = stochastic price process on real time market



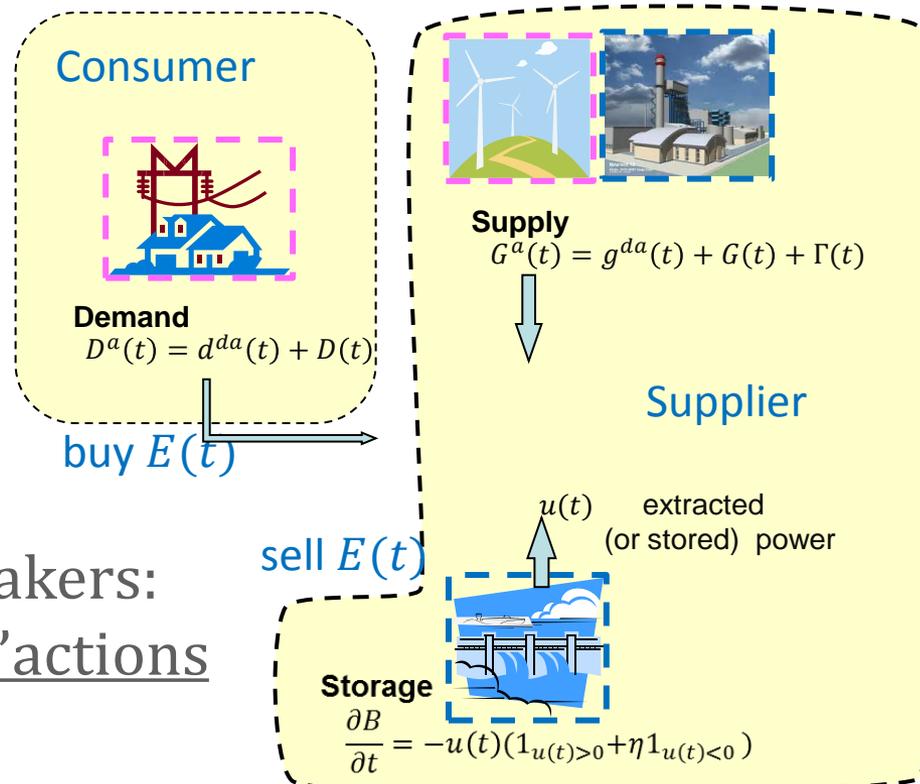
## Consumer's payoff

$$\underbrace{v \min(D^a(t), E(t) + g^{da}(t))}_{\text{satisfied demand}} - \underbrace{c^{bo}(D^a(t) - G^{da}(t) - -u(t))^+}_{\text{Frustrated demand}} - \underbrace{P(t)E(t) - p^{da}(t)g^{da}(t)}_{\text{Price paid}}$$

## Supplier's payoff

$$= P(t)E(t) + p^{da}(t)g^{da}(t) - cG(t) - c^{da}g^{da}(t)$$

# Definition of a competitive equilibrium



Assumption: agents are price takers:  
 $P(t)$  does not depend on players' actions

■  $(P, E, G, u)$  such that

1.  $E$  maximizes welfare (= expected discounted payoff) of consumer
2.  $E, G, u$  maximizes welfare of supplier (given friction constraints) for the same price process  $P$

■ Without storage, there exists such an equilibrium [Cho and Meyn 2010]

Other possible Storage owners

## B. Storage at Consumer

## C. Stand-alone storage operator

Consumer



Demand

$$D^a(t) = d^{da}(t) + D(t)$$

B.



Supplier

Supply

$$G^a(t) = g^{da}(t) + G(t) + \Gamma(t)$$



$u(t)$  extracted (or stored) power



Storage

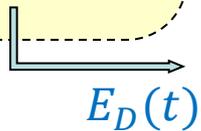
$$\frac{\partial B}{\partial t} = -u(t)(1_{u(t)>0} + \eta 1_{u(t)<0})$$

Consumer



Demand

$$D^a(t) = d^{da}(t) + D(t)$$



Supplier

Supply

$$G^a(t) = g^{da}(t) + G(t) + \Gamma(t)$$

$E_S(t)$

C.

$u(t)$  extracted (or stored) power

Storage

$$\frac{\partial B}{\partial t} = -u(t)(1_{u(t)>0} + \eta 1_{u(t)<0})$$

Storage operator

**Example:** Competitive equilibrium for scenario C:

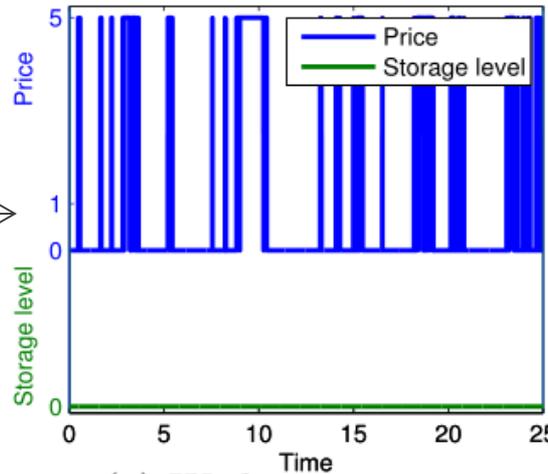
Storage Operator's payoff =  $u(t)P(t)$

Equilibrium:  $(P, E_D, E_S, G, u)$  such that

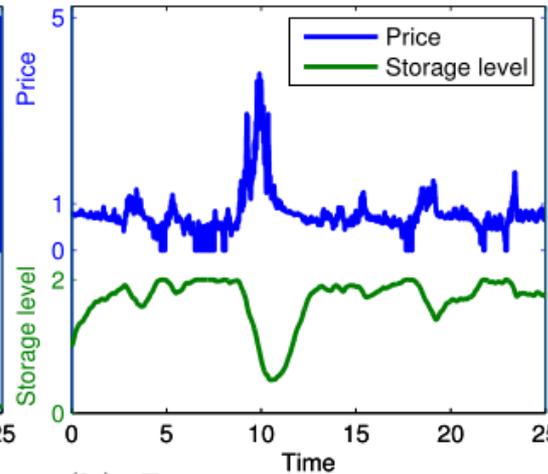
1.  $E_D$  maximizes consumer's welfare
2.  $E_S, G$  maximizes supplier's welfare
3.  $u$  maximizes storage op's welfare
4.  $E_D(t) + u(t) = E_S(t)$

# Dynamic Competitive Equilibria exist and are essentially the same for the 3 Scenarios [Theorem 3, Gast et al 2013]

No storage →



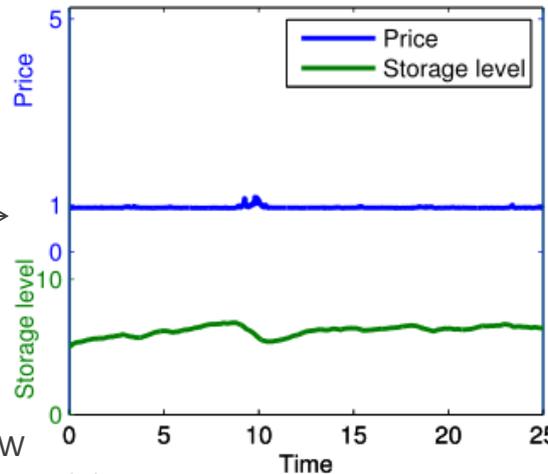
(a) Without storage



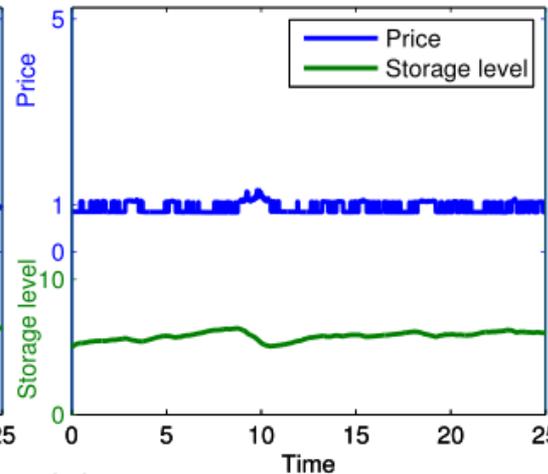
(b)  $B_{\max} = 2 \text{ u.e.}, \eta = 1.$

← Small storage

Large storage  
 $\eta = 1$  →



(c)  $B_{\max} = 10 \text{ u.e.}, \eta = 1$



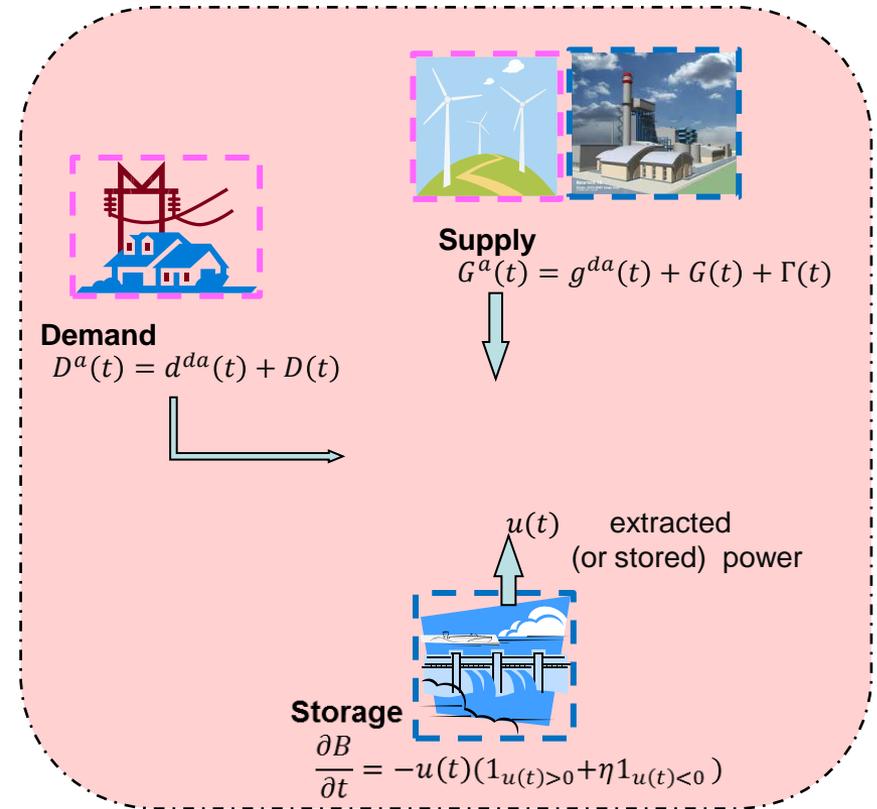
(d)  $B_{\max} = 10 \text{ u.e.}, \eta = 0.8$

← Large storage  
 $\eta = 0.8$

1 u.e. = 360 MWh, 1 u.p. = 600 MW  
 $\sigma^2 = 0.6 \text{ GW}^2/\text{h}, \zeta = 2 \text{ GW}/\text{h}$   
 $C_{\max} = D_{\max} = 3 \text{ u.p.}$

# The social planner problem

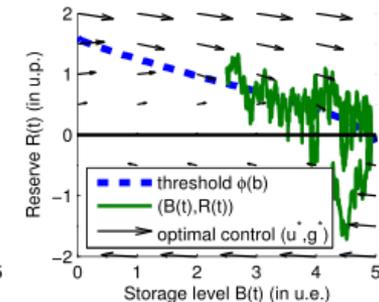
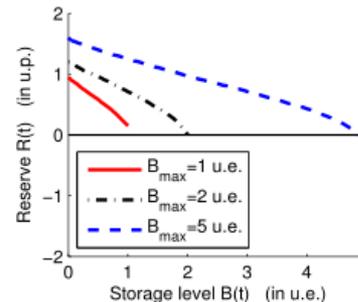
- The social planner wants to find  $G$  and  $u$  to maximize total expected discounted payoff
- Does not depend on storage owner



$$\underbrace{v \min(D^a(t), E(t) + g^{da}(t))}_{\text{satisfied demand}} - \underbrace{c^{bo} (D^a(t) - G^{da}(t) - u(t))^+}_{\text{Frustrated demand}} - \underbrace{cG(t) - c^{da} g^{da}(t)}_{\text{Cost of generation}}$$

- Let  $R(t) := G^a(t) + u(t) - D^a(t)$

Optimal control is such that:  
 if  $R(t) < \Phi(B(t))$  increase  $G(t)$   
 if  $R(t) > \Phi(B(t))$  decrease  $G(t)$



# The Social Welfare Theorem

## [Gast et al., 2013]

Any dynamic competitive equilibrium for any of the three scenarios maximizes social welfare

- ▶ The same price process controls optimally both the storage AND the production

As storage grows, prices concentrate on the marginal production cost if  $\eta = 1$

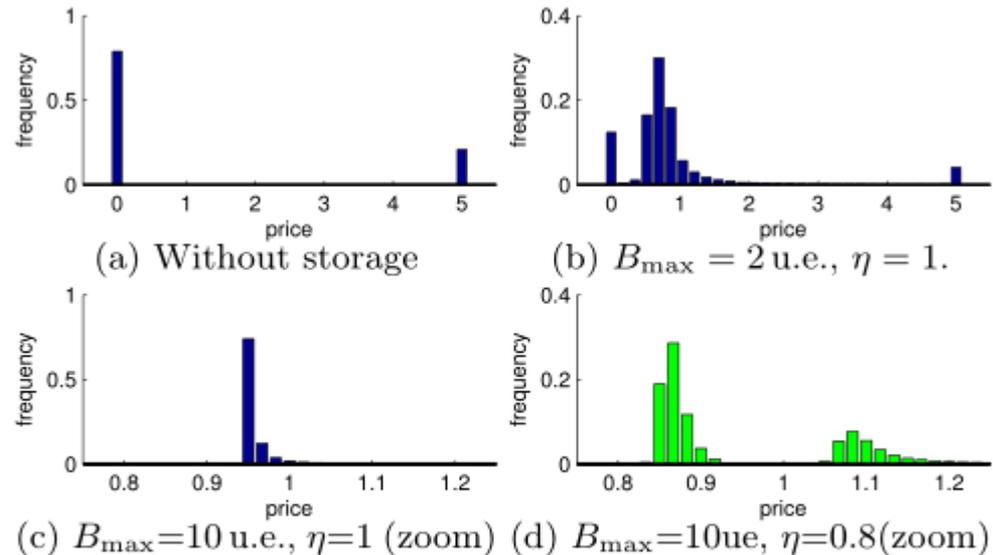
If  $\eta < 1$ : discontinuity in  $R(t)=0$

- ▶ Bad for decentralized control

Cycle efficiency

$$P^*(t) = \begin{cases} 0 & \text{Overproduction that storage cannot store} \\ \eta \frac{\partial V}{\partial b}(R^*(t), B^*(t)), & \text{Storage compensates fluctuations} \\ \frac{\partial V}{\partial b}(R^*(t), B^*(t)), & \\ v + c^{bo}, & \text{Underproduction that storage cannot satisfy} \end{cases}$$

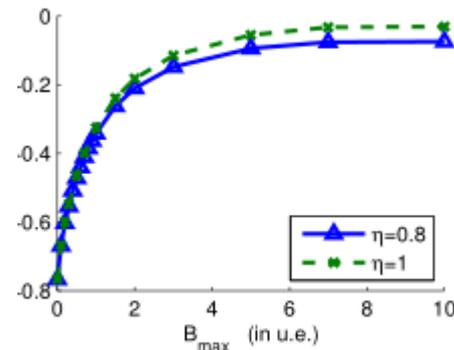
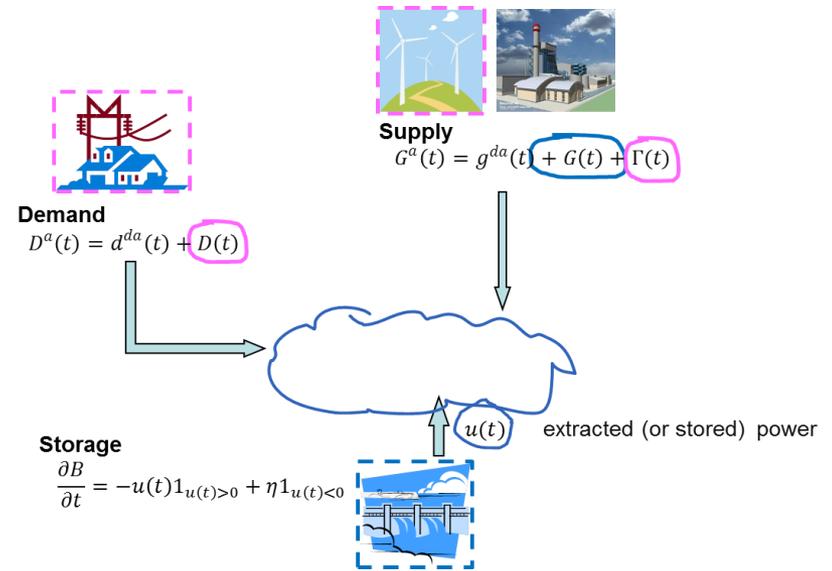
Prices are *dynamic* Lagrange multipliers



**Figure 6: Steady-state distribution of prices for various storage energy capacities  $B_{\max}$ . For  $B_{\max} = 10 \text{ u.e.}$ , we zoom on  $c=1$  to compare  $\eta = 0.8$  and  $\eta = 1$ .**

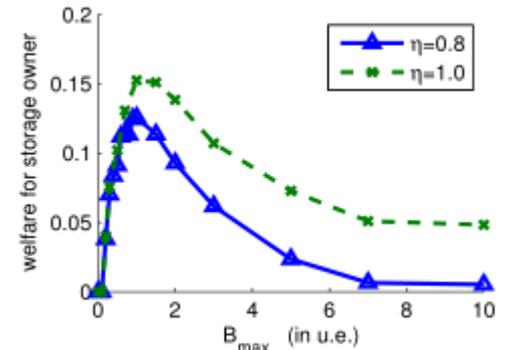
# The Invisible Hand of the Market may not be optimal

- Any dynamic competitive equilibrium for any of the three scenarios maximizes social welfare
- However, this assumes a given storage capacity.
- Is there an incentive to install storage ?
  - No, stand alone operators or consumers have no incentive to install the optimal storage



(b)  $C_{\max} = 3$  u.p.

Expected social welfare



(b)  $C_{\max} = D_{\max} = 3$  u.p.

Expected welfare of stand alone operator

Can lead to market manipulation  
(undersize storage and generators)

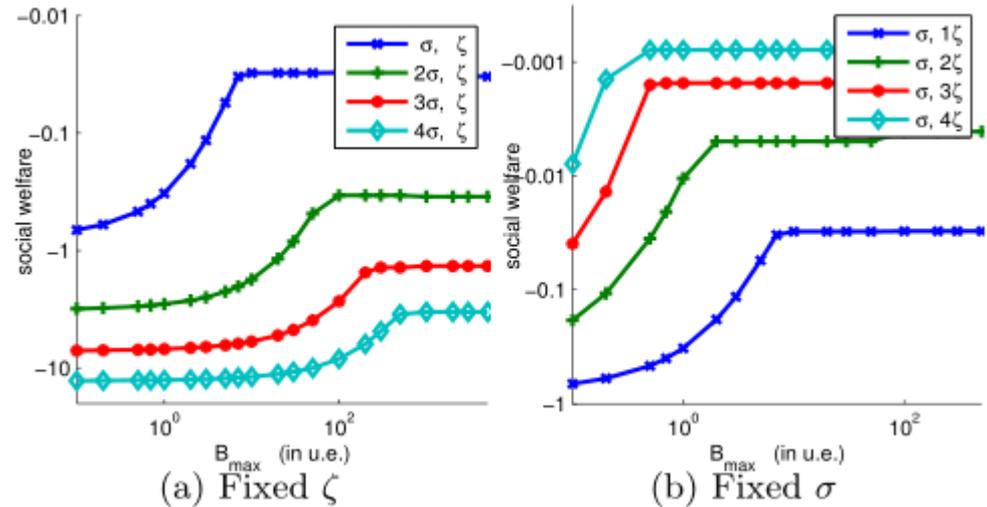
# Scaling laws and optimal storage sizing

■ (steepness) being close to social welfare requires the optimal storage capacity

■ optimal storage capacity scales like  $\frac{\sigma^4}{\zeta^3}$ !

( $\sigma$  is  $\approx$ proportional to the installed renewable capacity)

■ increase volatility and rampup capacity by  $x$   
= increase storage by  $x$



Bad news for renewables

(similar situation in Spain: for each 1MW of wind turbines, 1MW of gaz turbines in build!)

# What this suggests about storage :

- with a free and honest market, storage **can be** operated by prices
  - ▶ But prices are still volatile when  $\eta < 1$
- however, there may not be enough incentive for storage operators to install the optimal storage size
- perhaps preferential pricing should be directed towards storage as much as towards PV
  
- Multi temporal-scales are inherent to electricity networks
  - ▶ Joint scheduling is essential
  
- Limitation of the model / future work
  - ▶ Oligopolistic setting
  - ▶ Network constraints and distributed storage

# Thank You !

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